



# Neutrinoless double beta decays in left-right symmetric models (and more)

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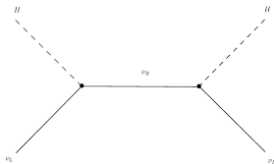
无中微子双贝塔衰变研讨会, 中山大学珠海校区

- Seesaw mechanisms and left-right symmetric model (LRSM)
- $0\nu\beta\beta$  in seesaw mechanisms
- $0\nu\beta\beta$  in LRSM
- Other probes of seesaw mechanisms and LRSM
  - ▶ low-energy high-precision MOLLER experiment
  - ▶ long-lived  $H_{L,R}^{\pm\pm}$  at high-energy colliders
  - ▶ Searches of  $N_i$  and  $W_R$  at high-energy colliders
- Conclusion

## Seesaw mechanisms & LRSM

# Type-I seesaw

Minkowski '77; Mohapatra & Senjanović '80; Yanagida '79;  
Gell-Mann, Ramond & Slansky '79; Glashow '80



- Basic Lagrangian to generate tiny neutrino masses

$$\mathcal{L} = -y_D \bar{L} \phi N + \frac{1}{2} \overline{N^c} M_N N$$

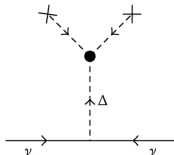
- Heavy-light neutrino mixing induced couplings

$$\mathcal{L} = -\frac{g}{\sqrt{2}} W_\mu \bar{\ell}_\alpha \gamma^\mu P_L [U_{\alpha i} \nu_i + V_{\alpha j} N_j]$$

The heavy-light neutrino mixing will induce contributions of heavy neutrinos to  $0\nu\beta\beta$ !

# Type-II seesaw

Konetschny & Kummer '77; Magg & Wetterich '80; Schechter & Valle '80;  
Cheng & Li '80; Mohapatra & Senjanovic '81; Lazarides, Shafi & Wetterich '81



- One of the simplest seesaw frameworks to generate the tiny neutrino masses...

$$\mathcal{L} = - (f_L)_{\alpha\beta} \psi_{L\alpha}^T C i \sigma_2 \Delta_L \psi_{L\beta} + \mu H^T i \sigma_2 \Delta_L^\dagger H + \text{H.c.},$$
$$\Delta_L = \begin{pmatrix} \delta_L^+ / \sqrt{2} & \delta_L^{++} \\ \delta_L^0 & -\delta_L^+ / \sqrt{2} \end{pmatrix}.$$

- Neutrino masses are given by

$$m_\nu = \sqrt{2} f_L \nu_L = U \hat{m}_\nu U^T \quad (\text{with the VEV } \langle \delta_L^0 \rangle = \nu_L / \sqrt{2})$$

- The coupling matrix  $f_L$  is fixed by neutrino oscillation data, up to the unknown lightest neutrino mass  $m_0$ , the neutrino mass hierarchy, and the Dirac & Majorana CP violating phases.

# Parity violation since 1957



Figure: C. N. Yang, T. D. Lee & C. S. Wu

Left  $\neq$  Right

# Parity restoration

*“As in my 1957 Rochester Conference lecture, we assume all  $P$ ,  $C$ ,  $T$  asymmetries observed are due to asymmetries in the solution — the asymmetries within our local big bang universe. **The fundamental equations of physics remain  $P$ ,  $C$ ,  $T$  symmetric.** Fifty years later, we may assume further that all such asymmetries are due to the spontaneous symmetry breaking mechanism generated by spin 0 Higgs field  $\phi$ . In such a picture, without  $\phi$  all spin nonzero fields would be symmetry conserving and of zero mass; these should include besides graviton and photon, also  $W^\pm$ ,  $Z^0$ , quarks and leptons.”*

— T. D. Lee, NPA **805** (2008) 54 [see also hep-ph/0605017]

(TeV-scale) left-right symmetric model:

Pati & Salam '74; Mohapatra & Pati '75; Senjanović & Mohapatra '75

$$SU(2)_L \times U(1)_Y \Rightarrow SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

other options of LRSM, e.g.  $SU(2)_L \times SU(2)_R \times U(1)_{Y_L} \times U(1)_{Y_R}$

Dev, Kazanas, Mohapatra, Teplitz & YCZ '16 [JCAP]; Dev, Mohapatra & YCZ '16 [JHEP]

# Left-Right Symmetric Model (LRSM)

Pati & Salam '74; Mohapatra & Pati '75; Senjanović & Mohapatra '75

- Heavy are added automatically to the SM:

$$Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \in \left( \mathbf{2}, \mathbf{1}, \frac{1}{3} \right) \xleftrightarrow{P} Q_R = \begin{pmatrix} u_R \\ d_R \end{pmatrix} \in \left( \mathbf{1}, \mathbf{2}, \frac{1}{3} \right)$$
$$\Psi_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \in (\mathbf{2}, \mathbf{1}, -1) \xleftrightarrow{P} \Psi_R = \begin{pmatrix} N_R \\ e_R \end{pmatrix} \in (\mathbf{1}, \mathbf{2}, -1)$$

- Electric charge and the hypercharge

$$Q = I_{3L} + I_{3R} + \frac{1}{2}(B - L)$$

- Tiny neutrino masses via seesaw mechanism(s) & heavy RHNs  $N$
- Heavy gauge bosons  $W_R$  and  $Z_R$  from the  $SU(2)_R \times U(1)_{B-L}$  sector.
- Heavy (and light) beyond SM scalars.



$$\begin{array}{c}
 SU(2)_L \times SU(2)_R \times U(1)_{B-L} \\
 \Downarrow \Delta_R(\mathbf{1}, \mathbf{3}, 2) \\
 SU(2)_L \times U(1)_Y \\
 \Downarrow \Phi(\mathbf{2}, \mathbf{2}, 0) \\
 U(1)_{EM}
 \end{array}$$

$$\begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_R^+ & \Delta_R^{++} \\ \Delta_R^0 & -\frac{1}{\sqrt{2}}\Delta_R^+ \end{pmatrix} \Rightarrow \begin{pmatrix} 0 & 0 \\ \langle \Delta_R^0 \rangle & 0 \end{pmatrix}$$

$$\Rightarrow H_3^0, H_2^{\pm\pm}$$

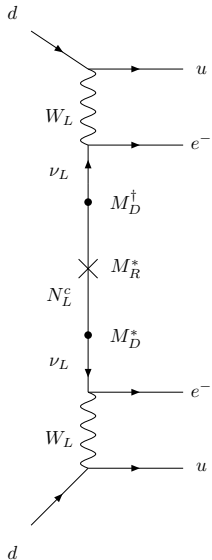
$$\begin{pmatrix} \phi_1^0 & \phi_2^+ \\ \phi_1^- & \phi_2^0 \end{pmatrix} \Rightarrow \begin{pmatrix} \langle \phi_1^0 \rangle & 0 \\ 0 & \langle \phi_2^0 \rangle \end{pmatrix}$$

$$\Rightarrow h, H_1^0, A_1^0, H_1^\pm$$

- Left-handed  $\Delta_L$  is used to enable type-II seesaw.
- Left-handed  $\Delta_L$  can decouple from the TeV scale physics:  
The parity restoration scale does not necessarily coincide with the  $SU(2)_R$  breaking scale. [Chang, Mohapatra & Parida '84, Deshpande, Gunion, Kayser & Olness '91]
- Other  $SU(2)_R$  breaking pattern: a right-handed doublet  $\phi_R$  [Babu & Mohapatra '89 [PRL]; '90 [PRD]].

$0\nu\beta\beta$  in seesaw mechanisms & LRSM

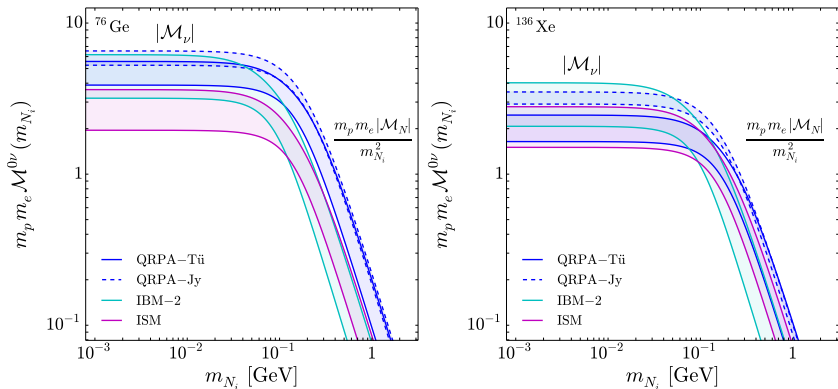
# $0\nu\beta\beta$ in type-I seesaw



Heavy-light neutrino mixing [Casas & Ibarra '01 [NPB]]

$$V_{eN_i} = i(U_{\text{PMNS}})_{ek} H_{kj} \sqrt{\frac{m_j}{m_{N_i}}} \mathcal{R}_{ij}^*$$

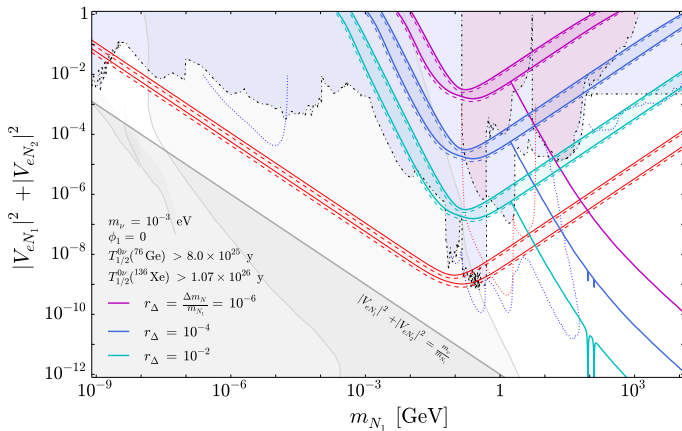
$U_{\text{PMNS}}$ : light neutrino mixing matrix;  
 $H$ : Hermitian matrix encoding deviations from unitarity in the light neutrino sector;  
 $m_j$ : light neutrino mass;  
 $m_{N_i}$ : heavy neutrino mass;  
 $\mathcal{R}$ : arbitrary  $2 \times 2$  orthogonal matrix



$$\sum_i \frac{m_i U_{ei}^2}{\langle \mathbf{p}^2 \rangle} + \sum_i \frac{m_{N_i} V_{eN_i}^2}{\langle \mathbf{p}^2 \rangle + m_{N_i}^2}$$

# $0\nu\beta\beta$ limits in type-I seesaw

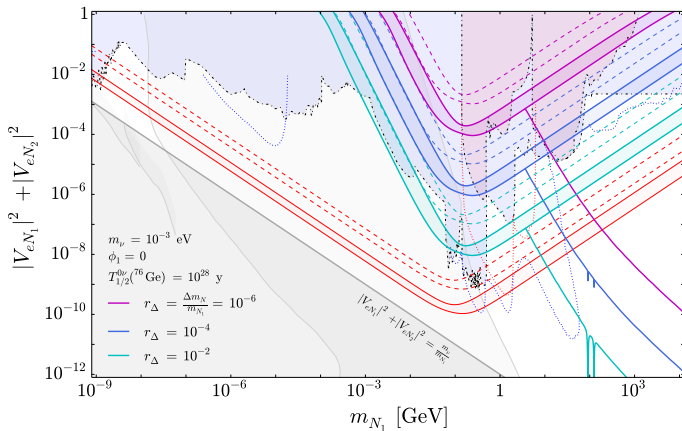
Bolton, Deppisch & Dev '20 [JHEP]



bands: uncertainties:  
 solid:  ${}^{136}\text{Xe}$ ; dashed:  ${}^{76}\text{Ge}$ ;  
 red: single heavy neutrino

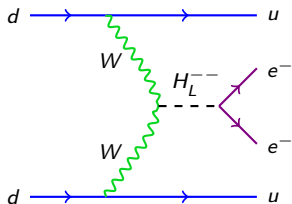
# Future $0\nu\beta\beta$ prospects in type-I seesaw

Bolton, Deppisch & Bhupal Dev '20 [JHEP]



bands: uncertainties:  
solid:  $^{136}\text{Xe}$ ; dashed:  $^{76}\text{Ge}$ ;  
red: single heavy neutrino

# $0\nu\beta\beta$ in type-II seesaw



The  $H_L^{\pm\pm}$  contribution is highly suppressed by

$$\frac{(f_L)_{ee} v_L}{M_{H_L^{\pm\pm}}^2}$$

# $0\nu\beta\beta$ in LRSM

Mohapatra & Vergados '81 [PRL]; Hirsch, Klapdor-Kleingrothaus & Panella '96 [PLB]; Dev, Goswami, Mitra & Rodejohann '13 [PRD]; Huang & Lopez-Pavon '14 [EPJC]; Dev, Goswami & Mitra '15 [PRD]; Deppisch, Gonzalo, Patra, Sahu & Sarkar '15 [PRD] Ge, Lindner & Patra '15 [JHEP]; Borah & Dasgupta '15 [JHEP]

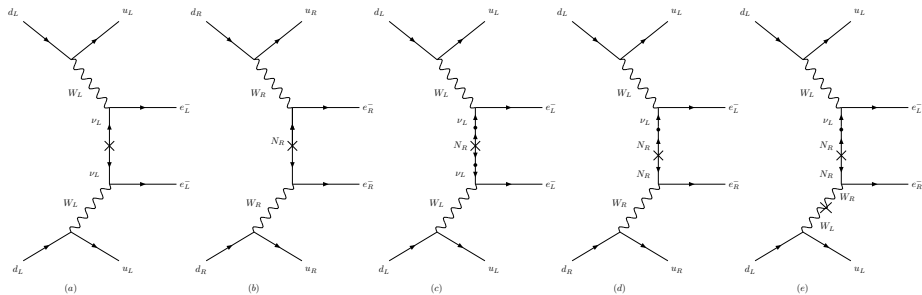


Figure: Contributions  $\mathcal{A}_\nu$ ,  $\mathcal{A}_{N_R}^R$ ,  $\mathcal{A}_{N_R}^L$ ,  $\mathcal{A}_\lambda$ ,  $\mathcal{A}_\eta$  to  $0\nu\beta\beta$  in LRSM



# Different contributions to $0\nu\beta\beta$

Different contributions to  $0\nu\beta\beta$  in LRSM

Dev, Goswami & Mitra '15 [PRD]

$$\eta_\nu = \frac{1}{m_e} \sum_i U_{ei}^2 m_i,$$

$$\eta_\lambda = \left( \frac{M_{W_L}}{M_{W_R}} \right)^2 \sum_i U_{ei} T_{ei}^*,$$

$$\eta_{N_R}^R = m_p \left( \frac{M_{W_L}}{M_{W_R}} \right)^4 \sum_i \frac{V_{ei}^{*2}}{M_i},$$

$$\eta_\eta = \tan \xi \sum_i U_{ei} T_{ei}^*,$$

$$\eta_{N_R}^L = m_p \sum_i \frac{S_{ei}^2}{M_i},$$

Neutrino mixing matrix

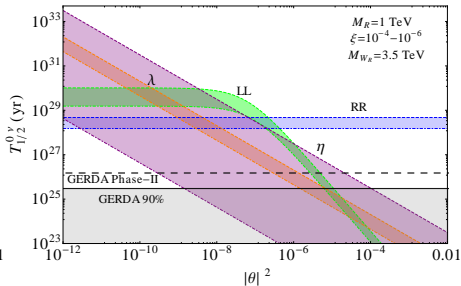
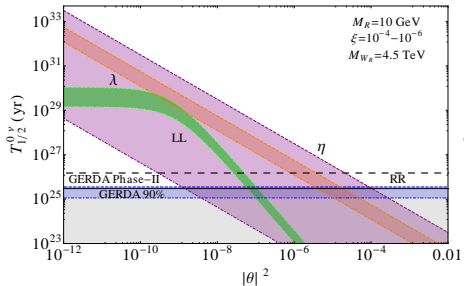
$$\mathcal{V} = \begin{pmatrix} U & S \\ T & V \end{pmatrix}, \quad S, T \sim iUH \sqrt{\frac{m_j}{M_i}} \mathcal{R}^*$$

$W - W_R$  mixing

$$\xi \simeq \frac{\kappa_1 \kappa_2}{v_R^2} \simeq \frac{2\kappa_2}{\kappa_1} \left( \frac{M_{W_L}}{M_{W_R}} \right)^2$$

# Different contributions to $0\nu\beta\beta$

Dev, Goswami & Mitra '15 [PRD]



# $0\nu\beta\beta$ limits on heavy-light neutrino mixing angle

Dev, Goswami & Mitra '15 [PRD]

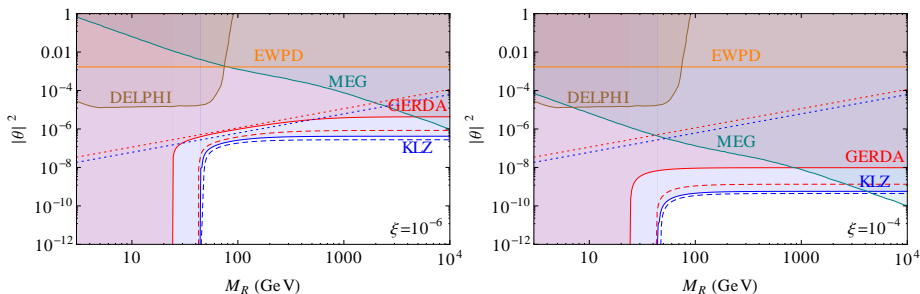
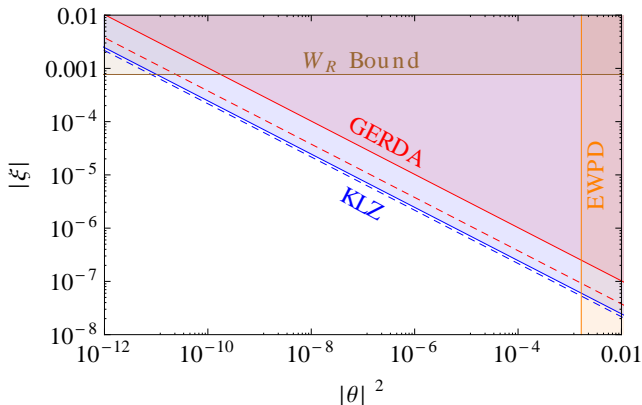


Figure: Setting  $M_{W_R} = 3.5$  TeV [ATLAS, 1809.11105; 1904.12679]

- Dotted lines: Standard seesaw with only LL contribution;
- Solid/dashed: NME uncertainties;
- DELPHI:  $Z$  decay limits;
- EWPD: Electroweak precision data limits;
- MEG:  $\text{BR}(\mu \rightarrow e\gamma)$  limits.

# $0\nu\beta\beta$ limits on $W - W_R$ mixing

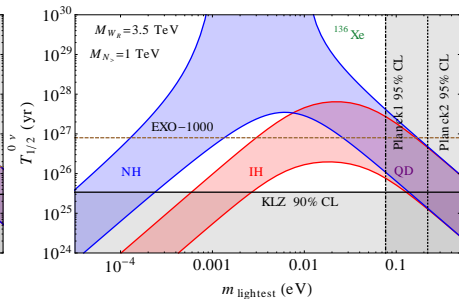
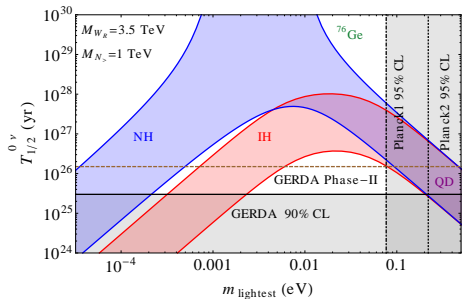
Dev, Goswami & Mitra '15 [PRD]



- Solid/dashed: NME uncertainties;
- $W_R$  limits 3.8 - 5 TeV for  $100 \text{ GeV} < m_N < 1.8 \text{ TeV}$  [ATLAS, 1809.11105; 1904.12679];
- EWPD: Electroweak precision data limits.

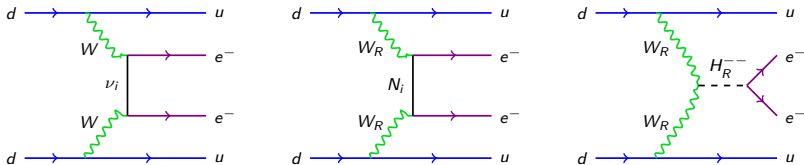
# $0\nu\beta\beta$ limits on $m_0$

Dev, Goswami & Mitra '15 [PRD]



# $0\nu\beta\beta$ in LRSM: $H_R^{\pm\pm}$ contribution

Mohapatra & Vergados '81 [PRL]; Hirsch, Klapdor-Kleingrothaus & Panella '96 [PLB]; Dev, Goswami, Mitra & Rodejohann '13 [PRD]; Huang & Lopez-Pavon '14 [EPJC]; Dev, Goswami & Mitra '15 [PRD]; Deppisch, Gonzalo, Patra, Sahu & Sarkar '15 [PRD] Ge, Lindner & Patra1 '15 [JHEP]; Borah & Dasgupta '15 [JHEP]



Neglecting the contributions due to  $W - W_R$  mixing and heavy-light neutrino mixing.  
 The  $H_L^{\pm\pm}$  contribution is highly suppressed by  $(f_L)_{ee} \nu_L / M_{H_L^{\pm\pm}}^2$

# $0\nu\beta\beta$ in LRSM: $H_R^{\pm\pm}$ contribution

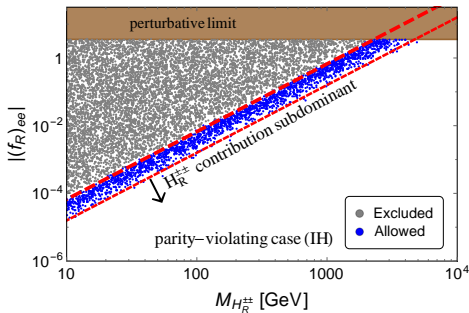
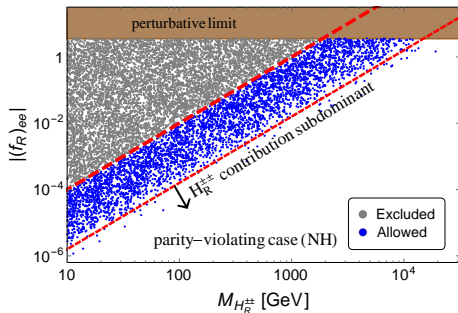
Barry & Rodejohann '13 [JHEP]; Dev, Ramsey-Musolf & YCZ '18 [PRD]

RR and  $H_R^{\pm\pm}$  contributions:

$$\begin{aligned}\eta_N &= m_p \left(\frac{g_R}{g_L}\right)^4 \left(\frac{m_W}{M_{W_R}}\right)^4 \sum_i \frac{V_{ei}^2}{M_{N_i}} \\ &= \frac{m_p}{4} \left(\frac{v_{EW}}{v_R}\right)^4 \sum_i \frac{V_{ei}^2}{M_{N_i}}, \\ \eta_{\delta_R} &= m_p \left(\frac{g_R}{g_L}\right)^4 \left(\frac{m_W}{M_{W_R}}\right)^4 \frac{\sqrt{2}(f_R)_{ee} v_R}{M_{H_R^{\pm\pm}}^2} \\ &= \frac{m_p}{2\sqrt{2}} \left(\frac{v_{EW}}{v_R}\right)^4 \frac{(f_R)_{ee} v_R}{M_{H_R^{\pm\pm}}^2}, \\ \frac{\eta_N}{\eta_{\delta_R}} &\sim \frac{M_{N_i}^2}{M_{H_R^{\pm\pm}}^2}\end{aligned}$$

# $H_R^{\pm\pm}$ contribution to $0\nu\beta\beta$

Dev, Ramsey-Musolf & YCZ '18 [PRD]



$$v_R = 5\sqrt{2} \text{ TeV};$$

$f_L \neq f_R$  in parity-violating LRSM:

the couplings of heavy neutrinos are free parameters.

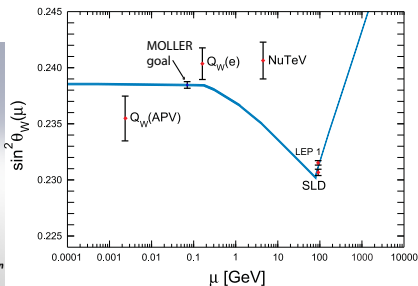
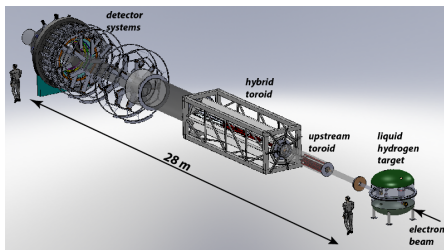


$H^{\pm\pm}$  @ MOLLER experiment

# MOLLER experiment

## (Measurement Of a Lepton Lepton Electroweak Reaction)

MOLLER Collaboration, 1411.4088; [https://moller.jlab.org/moller\\_root/](https://moller.jlab.org/moller_root/)



Primary Goal:

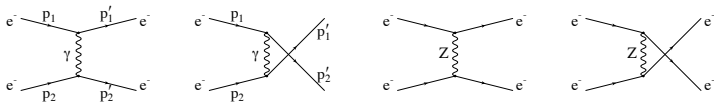
Precision measurement of  $A_{PV}$  to the level of 0.7 ppb ( $A_{PV}^{\text{SM}} \simeq 33$  ppb);

An overall fractional accuracy of 2.4% for  $Q_W^e$ .

# Parity-violating asymmetry

MOLLER Collaboration, 1411.4088; [https://moller.jlab.org/moller\\_root/](https://moller.jlab.org/moller_root/)

Scattering of longitudinally polarized electrons off unpolarized electrons, using the upgraded 11 GeV beam in Hall A at JLab



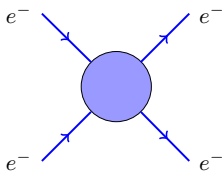
$$A_{\text{PV}} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = \frac{G_F m_e E}{\sqrt{2}\pi\alpha} \frac{2y(1-y)}{1+y^4 + (1-y)^4} Q_W^e,$$

$E(E')$ : incident beam (scattered electron) energy;  $y = 1 - E'/E$ ;

$$Q_W^e = 1 - 4\sin^2\theta_W \text{ (tree level)}$$

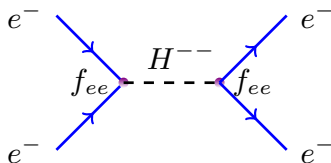
# Sensitivity to four-electron contact interaction

MOLLER Collaboration, 1411.4088



$$\frac{\Lambda}{\sqrt{|g_{RR}^2 - g_{LL}^2|}} = \frac{1}{\sqrt{\sqrt{2}G_F|\Delta Q_W^e|}} \simeq 7.5 \text{ TeV},$$

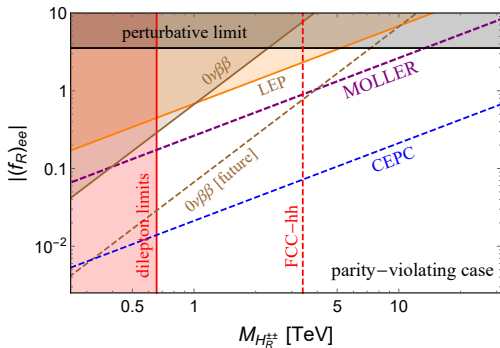
# Sensitivity to doubly-charged scalar



$$\mathcal{M}_{\text{PV}} \sim \frac{|(f_L)_{ee}|^2}{2M_{H_L^{\pm\pm}}^2} (\bar{e}_L \gamma^\mu e_L)(\bar{e}_L \gamma_\mu e_L) + (L \leftrightarrow R).$$

Keeping only the left-handed part:  $|g_{LL}|^2 = |(f_L)_{ee}|^2/2$  &  $g_{RR} = 0$ :

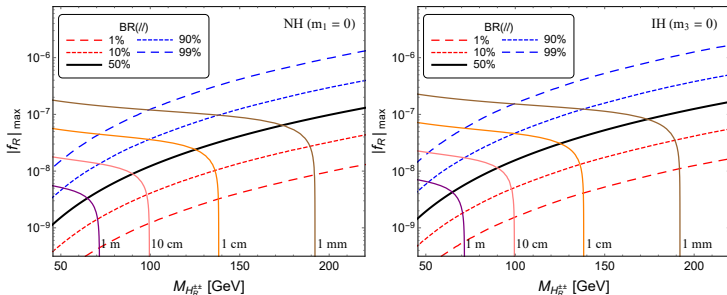
$$\frac{M_{H_L^{\pm\pm}}}{|(f_L)_{ee}|} \gtrsim 3.7 \text{ TeV} \quad (\text{at the 95\% C.L.})$$



dilepton limits: direct LHC searches;  
 LEP:  $e^+e^- \rightarrow e^+e^-$  limits;  
 CEPC: luminosity =  $1 \text{ ab}^{-1}$ ;  
 FCC-hh: luminosity =  $30 \text{ ab}^{-1}$

Long-lived  $H_R^{\pm\pm}$  in LRSM

# Proper lifetime of $H_R^{\pm\pm}$



$$\Gamma_{\text{total}}(H_R^{\pm\pm}) = \Gamma(H_R^{\pm\pm} \rightarrow \ell_\alpha^\pm \ell_\beta^\pm) + \Gamma(H_R^{\pm\pm} \rightarrow W_R^{\pm*} W_R^{\pm*}).$$

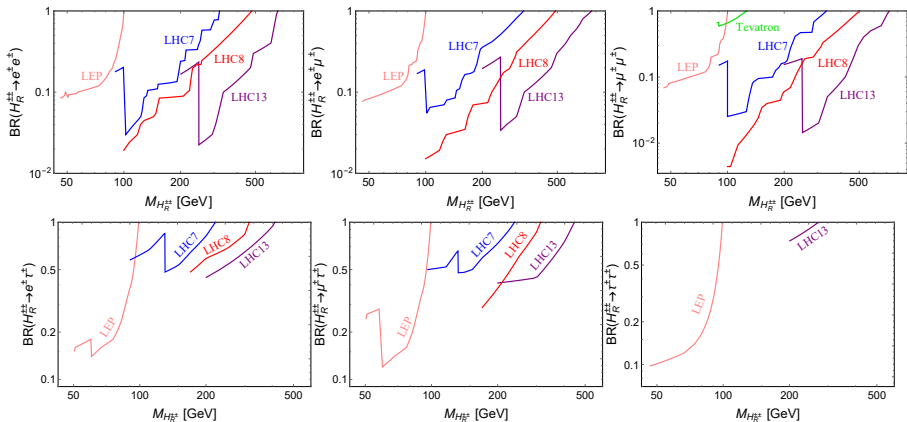
Assuming lightest neutrino mass  $m_0 = 0$ .

Assuming  $f_L = f_R$ ,  $g_L = g_R$  and  $v_R = 5\sqrt{2}$  TeV.

$H_R^{\pm\pm} \rightarrow W_R^{\pm*} W_R^{\pm*}$  highly suppressed by  $W_R$  mass.



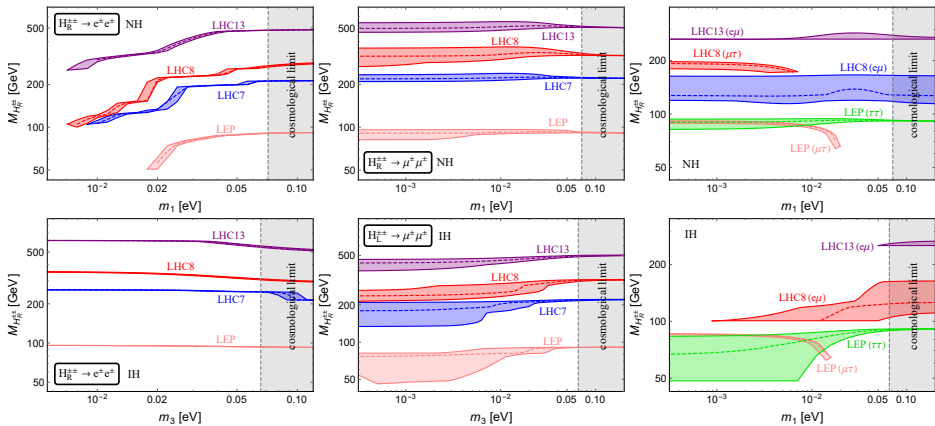
# Same-sign dilepton constraints on $H_R^{\pm\pm}$



OPAL, hep-ex/0111059; DELPHI, hep-ex/0303026; L3, hep-ex/0309076;  
 CDF, hep-ex/0406073; 0808.2161; D0, 0803.1534; 1106.4250;  
 ATLAS, ATLAS-CONF-2011-127; 1412.0237; 1710.09748;  
 CMS, CMS-PAS-HIG-11-007; CMS-PAS-HIG-14-039; CMS-PAS-HIG-16-036

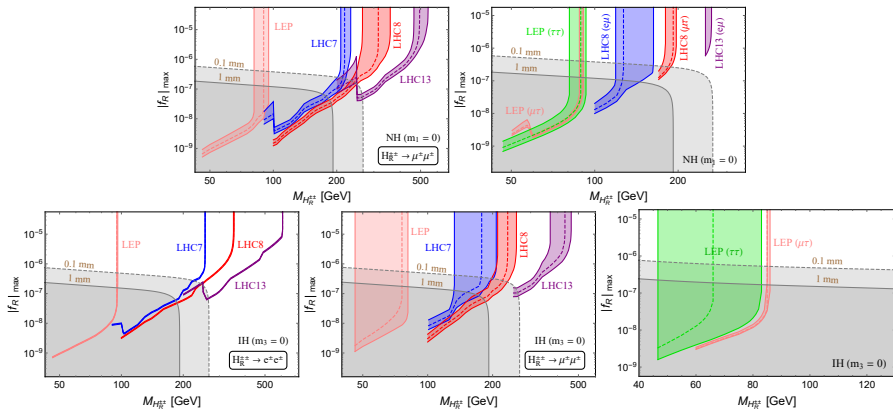
To some extent weaker than the  $H_L^{\pm\pm}$  limits

# Lower limit on $H_R^{\pm\pm}$ mass in the limit of large $\nu_R$



Predominant decay mode  $H_R^{\pm\pm} \rightarrow \ell_{\alpha}^{\pm} \ell_{\beta}^{\pm}$

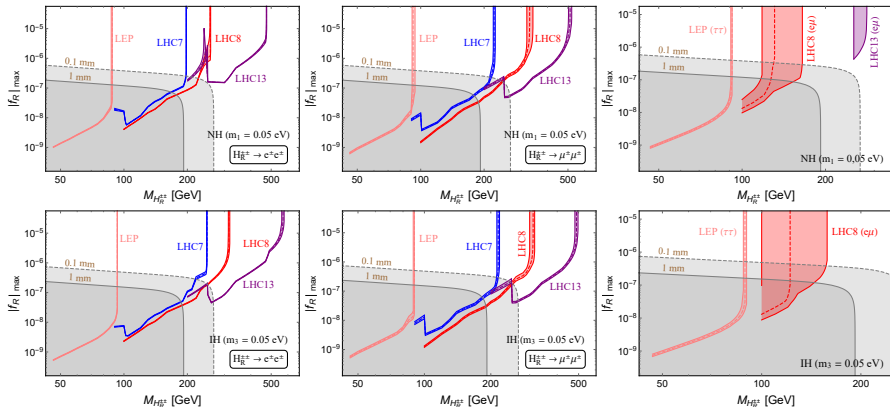
# Lower limit on $H_R^{\pm\pm}$ mass ( $m_0 = 0$ )



$$H_R^{\pm\pm} \rightarrow \ell_\alpha^\pm \ell_\beta^\pm, W_R^{\pm*} W_R^{\pm*}$$

Dashed lines: central values of neutrino oscillation data;  
Colorful bands:  $3\sigma$  uncertainties

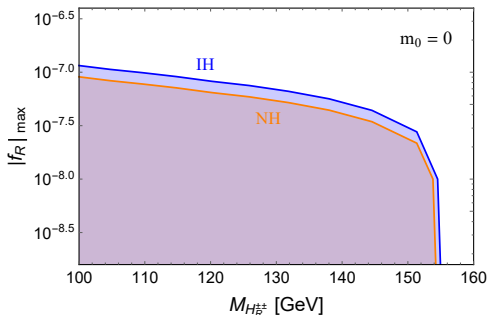
# Lower limit on $H_R^{\pm\pm}$ mass ( $m_0 = 0.05$ eV)



$$H_R^{\pm\pm} \rightarrow \ell_\alpha^\pm \ell_\beta^\pm, W_R^{\pm*} W_R^{\pm*}$$

Dashed lines: central values of neutrino oscillation data;  
Colorful bands:  $3\sigma$  uncertainties

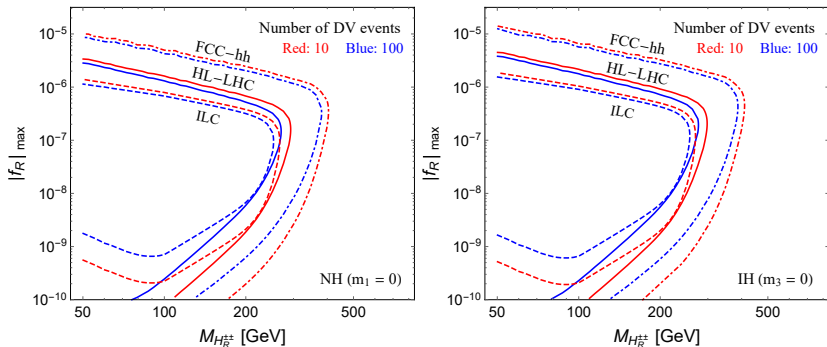
# Heavy stable charged particle (HSCP) constraints on $H_R^{\pm\pm}$



- Long-lived  $H_R^{\pm\pm}$  decays outside either the inner silicon tracker or the whole detector.
- We use conservatively only the “tracker-only” analysis.
- The decay length  $43 \text{ mm} < bc\tau_0(H_R^{\pm\pm}) < 1100 \text{ mm}$ .

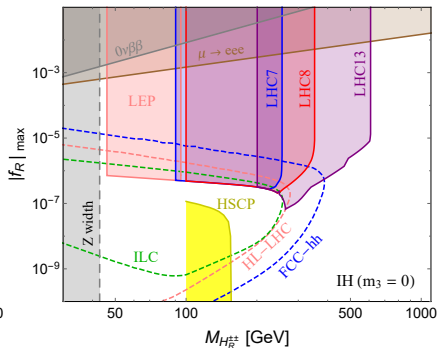
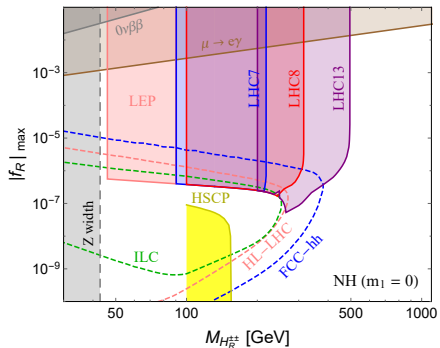
Very different from the  $H_L^{\pm\pm}$  case

# Displaced vertex (DV) prospects of $H_R^{\pm\pm}$



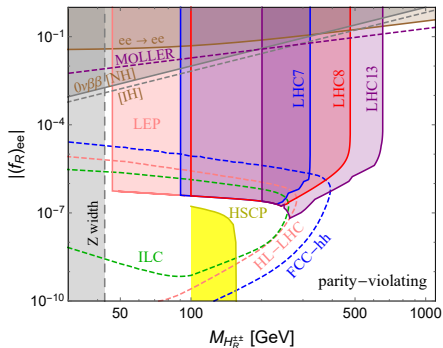
- Counting only the decays  $H_L^{\pm\pm} \rightarrow e^\pm e^\pm, e^\pm \mu^\pm, \mu^\pm \mu^\pm$ ;
- Setting  $g_R = g_L$  and the right-handed scale  $v_R = 5\sqrt{2}$  TeV.

# $0\nu\beta\beta$ limits vs. other limits/prospects



- Assuming at least 100 events for the DV sensitivities.
- The low-energy high-precision LFV measurements (such as  $\mu \rightarrow eee$ ,  $\mu \rightarrow e\gamma$  and  $0\nu\beta\beta$ ), the prompt same-sign dilepton searches of  $H_R^{\pm\pm}$  and the DV searches of  $H_R^{\pm\pm}$  are largely complementary to each other in the LRSM.

# ...for parity-violating LRSM

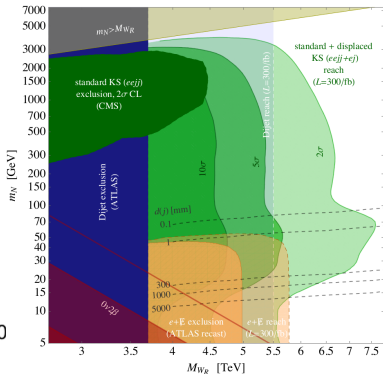
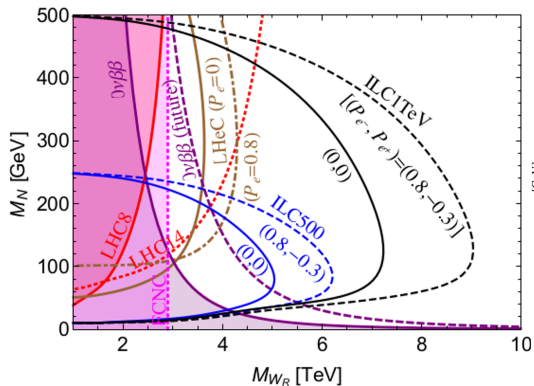


- Considering the simple scenario  $H_R^{\pm\pm} \rightarrow e^\pm e^\pm, W_R^{\pm*} W_R^{\pm*}$ .
- We do not have the LFV constraints e.g.  $\mu \rightarrow e\gamma$ , and MOLLER pops out...
- The low-energy high-precision LFV measurements (MOLLER and  $0\nu\beta\beta$ ), the prompt same-sign dilepton searches of  $H_R^{\pm\pm}$  and the DV searches of  $H_R^{\pm\pm}$  are largely complementary to each other in the LRSM.



# Complementarity of $N - W_R$ searches

Biswal & Dev '17 [PRD]; Nemevek, Nesti & Popara '18 [PRD]



# Conclusion

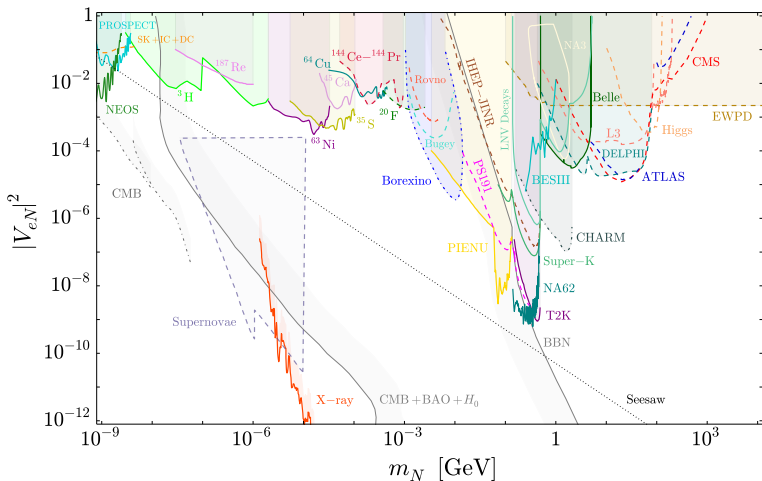
- In type-I seesaw and (minimal) LRSM, the contributions of  $N_i$  and  $H_R^{\pm\pm}$  to  $0\nu\beta\beta$  decays could be significant, depending on model details.
- The contributions of  $H_L^{\pm\pm}$  to  $0\nu\beta\beta$  is highly suppressed by  $\nu_L$  in type-II seesaw and LRSM.
- The  $0\nu\beta\beta$  prospects of  $N$ ,  $W_R$  and  $H_R^{\pm\pm}$  can be cross checked in other experiments, such as MOLLER and direct searches at high-energy colliders.

Thank you for your attention!

backup slides

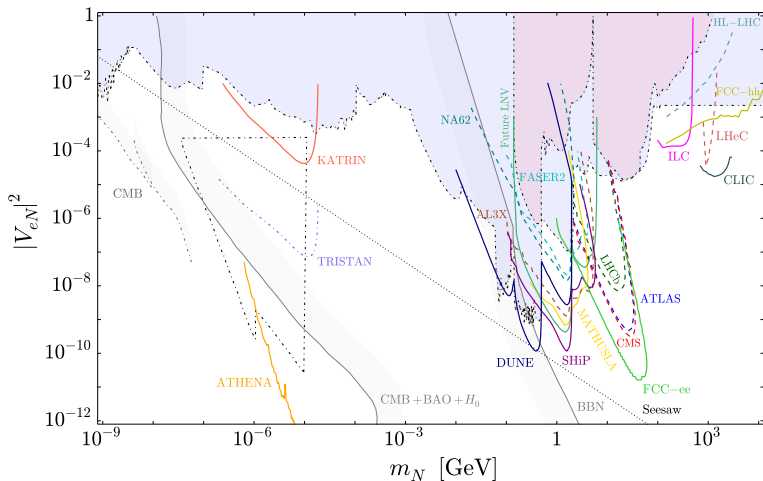
# Heavy-light neutrino mixing limits

Bolton, Deppisch & Dev '20 [JHEP]



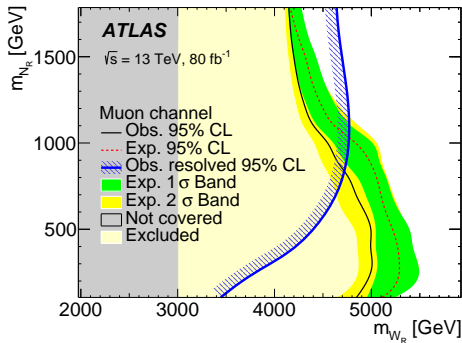
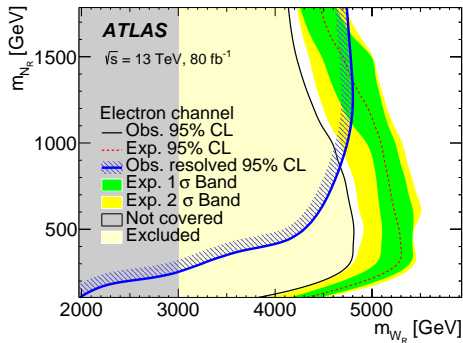
# Heavy-light neutrino mixing prospects

Bolton, Deppisch & Dev '20 [JHEP]



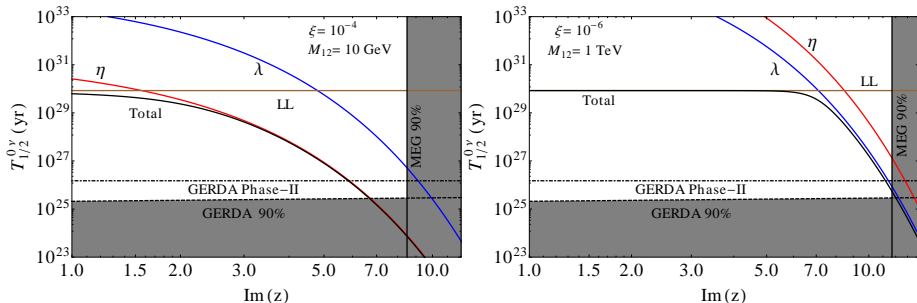
# LHC limits on $N_R$ and $W_R$

ATLAS, 1904.12679



# Different contributions to $0\nu\beta\beta$

Dev, Goswami & Mitra '15 [PRD]

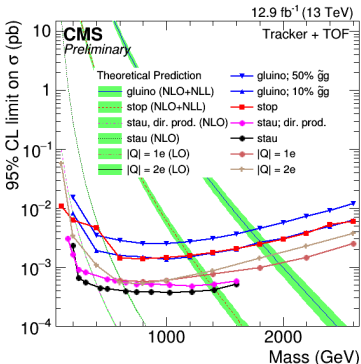
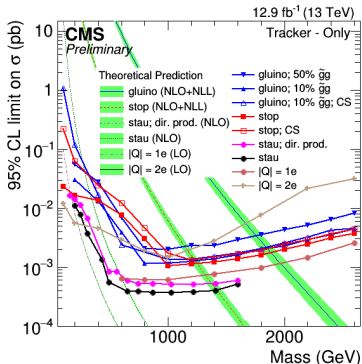


Arbitrary orthogonal matrix:

$$R = \begin{pmatrix} 0 & \cos z & -\sin z \\ 0 & \sin z & \cos z \\ 1 & 0 & 0 \end{pmatrix}$$

# Heavy Stable Charged particle (HSCP) searches

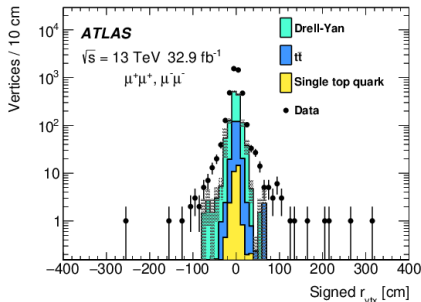
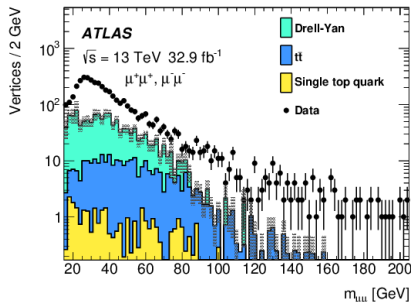
CMS-PAS-EXO-16-036





# Displaced same-sign dilepton searches: SM backgrounds

ATLAS, 1808.03057



- Dominant background: low-mass Drell-Yan processes  $pp \rightarrow e^+e^-, \mu^+\mu^-,$  with the charges of the electron or muon misidentified (and the electron misidentified as a muon or vice versa), depending largely on  $m_{\ell\ell'}$  and  $r_{vtx}$ .
- The dileptons from Drell-Yan processes tend to be back-to-back, which could be easily distinguished from the four-body process  $pp \rightarrow H_L^{++}H_L^{--} \rightarrow \ell_\alpha^\pm \ell_\beta^\pm \ell_\gamma^\mp \ell_\delta^\mp.$