



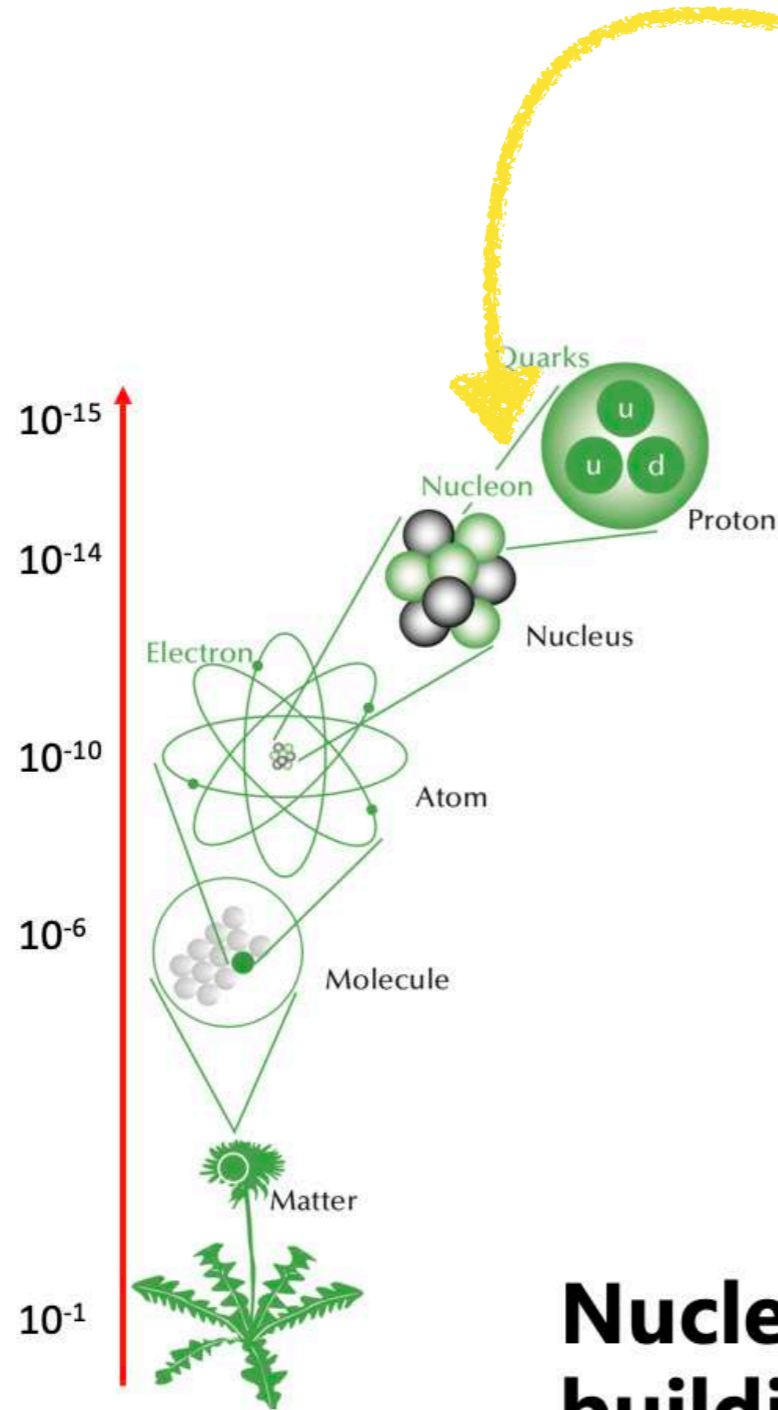
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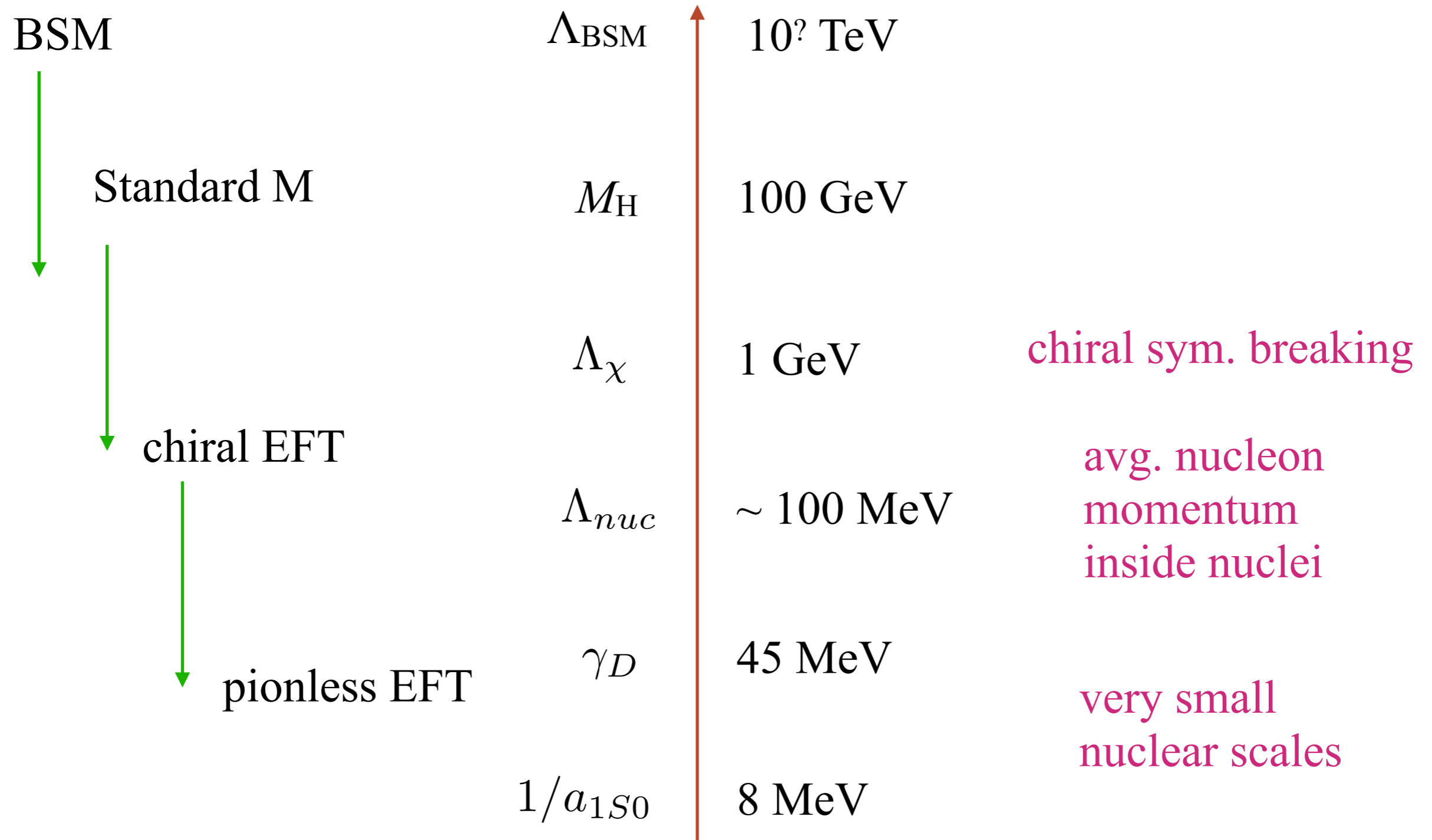
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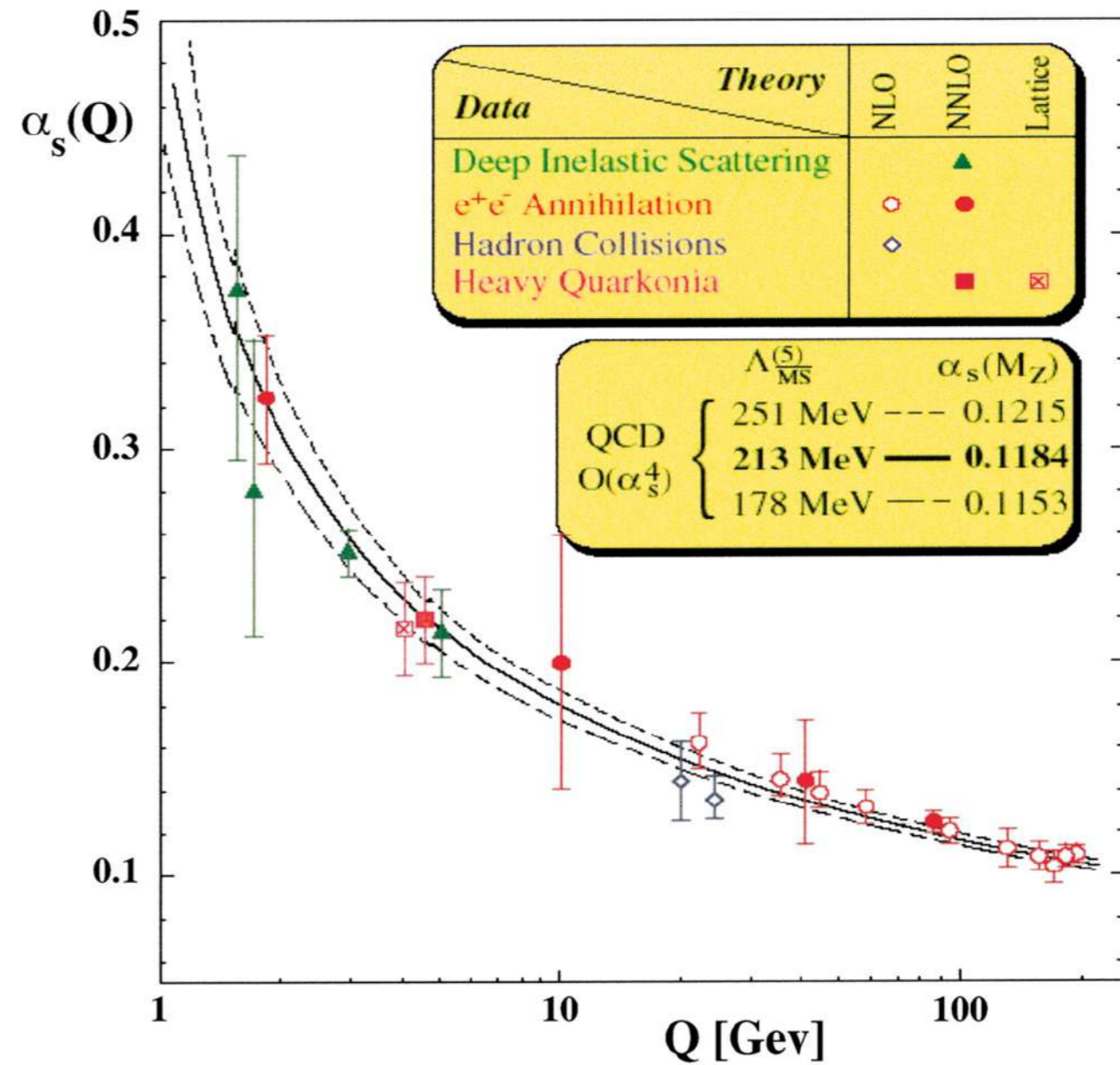


Nucleons are the essential building blocks of Matter!

BSM nuclear physics



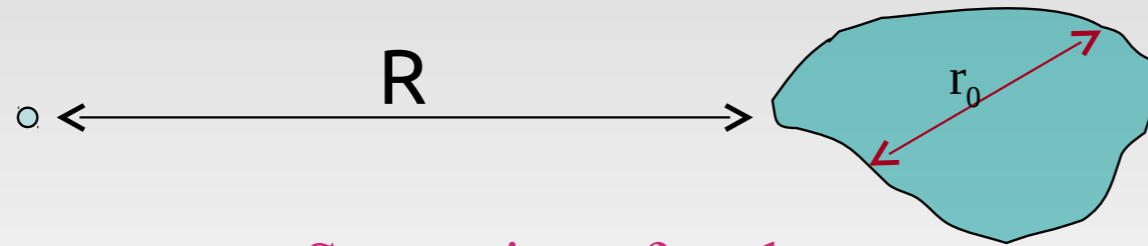
Perturbative QCD N/A



Nucl-ex/th is here!

What is EFT - a classical example

multipole expansions in electrodynamics
Charge distribution



Separation of scales

Symmetries of E&M
(Without knowing $\rho(\mathbf{R})$)

$\longrightarrow R \gg r_0$

$$V = \frac{q}{R} + \frac{d_i R_i}{R^3} + \frac{Q_{ij} R_i R_j}{R^5} + \dots$$

Low energy constants
(LECs)

$$\left. \begin{aligned} |d_i| &\sim q r_0 \\ |Q_{ij}| &\sim q r_0^2 \end{aligned} \right\}$$

Power counting

Based on dimensional analysis

Systematic low-energy approximation



$$V = \frac{q}{R} \left[1 + \mathcal{O}\left(\frac{r_0}{R}\right) + \mathcal{O}\left(\frac{r_0^2}{R^2}\right) + \dots \right]$$

Much more nontrivial in quantum systems!

Chiral EFT

- Low-energy approximation of QCD, expansion in Q/M_{hi}
Q: small external momenta
 M_{hi} : EFT breakdown scale (~ 500 MeV?)

$$\mathcal{M} = \sum_n \left(\frac{Q}{M_{hi}} \right)^n \mathcal{F}_n \left(\frac{Q}{M_{lo}} \right)$$

Q: generic external momenta,
 $M_{hi} = \Lambda_{SB}, m_\rho, \dots \sim 1\text{GeV}$
 $M_{lo} = m_\pi, f_\pi \sim 100\text{MeV}$

Systematic approximation

→ able to estimate theoretical errors

Chiral EFT

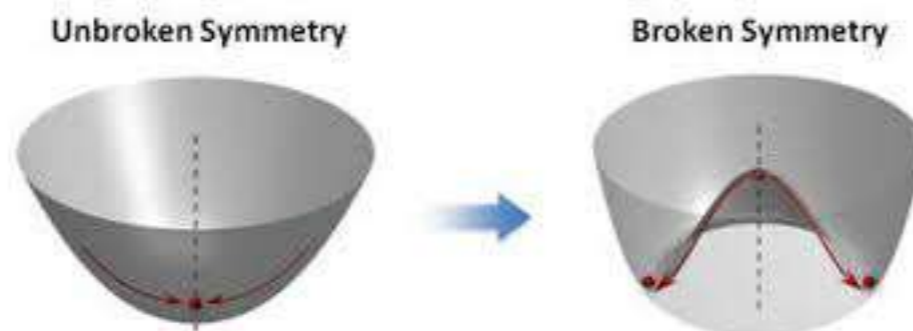
- Includes all symmetries of QCD, especially (approximate) chiral symmetry and its spontaneous breaking

$$\mathcal{L}_{\text{QCD}} = \sum_{f=u,d,s} \bar{q}_f (i\not{D} - m_f) q_f - \frac{1}{4} \mathcal{G}_{a\mu\nu} \mathcal{G}_a^{\mu\nu}$$

$$q_L \equiv \begin{pmatrix} u_L \\ d_L \\ s_L \end{pmatrix} \mapsto \left(\text{SU}(3)_L \right) \begin{pmatrix} u_L \\ d_L \\ s_L \end{pmatrix} \quad q_R \equiv \begin{pmatrix} u_R \\ d_R \\ s_R \end{pmatrix} \mapsto \left(\text{SU}(3)_R \right) \begin{pmatrix} u_R \\ d_R \\ s_R \end{pmatrix}$$

- Only two flavors used in our work

Lagrangian invariant when $m_f \rightarrow 0$, but broken by QCD ground state



→ chiral symmetry nonlinearly realized by hadronic Dofs

CCWZ; Weinberg; ...

Chiral EFT

- The most general Lagrangian has infinitely many parameters



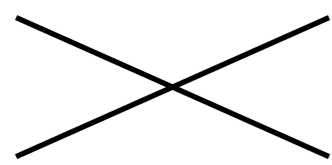
$$-\frac{g_A}{2f_\pi} N^\dagger \tau_a \vec{\sigma} \cdot \vec{\nabla} \pi_a N$$



$$-\frac{1}{4f_\pi^2} N^\dagger \epsilon_{abc} \tau_a \pi_b \dot{\pi}_c N$$

...

- Short-range interactions: large numbers of $4N$ operators



$$\begin{aligned}
 & -C^{(s)}(N^T P_i^{(s)} N)^\dagger (N^T P_i^{(s)} N) - C_2^{(s)} \left[(N^T P_i^{(s)} N)^\dagger (N^T P_i^{(s')} \overleftrightarrow{\nabla}^2 N) + h.c. \right] \dots \\
 & -C^{(ss')} (N^T P_i^{(s)} N)^\dagger (N^T P_i^{(s')} N) \dots
 \end{aligned}$$

$$P_i^{(1S_0)} = \frac{(i\sigma_2)(i\tau_2\tau_i)}{2\sqrt{2}}$$

$$\mathbf{s}, \mathbf{s}' = 1\mathbf{S}_0, 3\mathbf{S}_1, 3\mathbf{P}_0, \dots \quad P_i^{(3S_1)} = \frac{(i\sigma_2\sigma_i)(i\tau_2)}{2\sqrt{2}}$$

$$P_i^{(3D_1)} = \left(\overleftrightarrow{\nabla}_i \overleftrightarrow{\nabla}_j - \frac{\delta_{ij}}{n} \overleftrightarrow{\nabla}^2 \right) P_j^{(3S_1)}$$

**NN contact
pot. in mom.
space**

$$V_{1S_0} = c_0^{1S_0} + c_2^{1S_0}(p^2 + p'^2) + \dots$$

$$V_{3P_0} = c_0^{3P_0} pp' + \dots$$

Naive dim. analysis (NDA):

$$c_2^{1S_0} \sim c_0^{3P_0} \sim \frac{c_0^{1S_0}}{M_{hi}^2}$$

Power counting: long-range physics

Typical size of external momenta: $Q \sim m_\pi$

$$\begin{array}{c}
 \text{---} \\
 | \\
 \text{---}
 \end{array}
 \sim \frac{1}{f_\pi^2} \frac{Q^2}{m_\pi^2 + Q^2} \sim \frac{1}{f_\pi^2}
 \quad
 \begin{array}{c}
 \text{---} \\
 | \\
 \text{---} \\
 | \\
 \text{---}
 \end{array}
 \sim \frac{1}{f_\pi^2} \frac{m_N}{4\pi f_\pi} \frac{Q}{a_l f_\pi}$$

NN reducible

- Focus on loop momenta \sim external momenta Q
- Pion line or photon line $\sim 1/Q^2$, nucleon line in **irreducible** diagrams $\sim 1/Q$
- Nucleon line in **reducible** diagrams $\sim m_N/Q^2$
 - \Rightarrow Explain why we solve the Schrodinger eqn
 - \Rightarrow Explain why nuclei bound
- Strength of OPE $\sim a_l f_\pi$ (numerical factor $a_l \sim 1$ for small l , $a_l \gg 1$ for large l by centrifugal suppression)

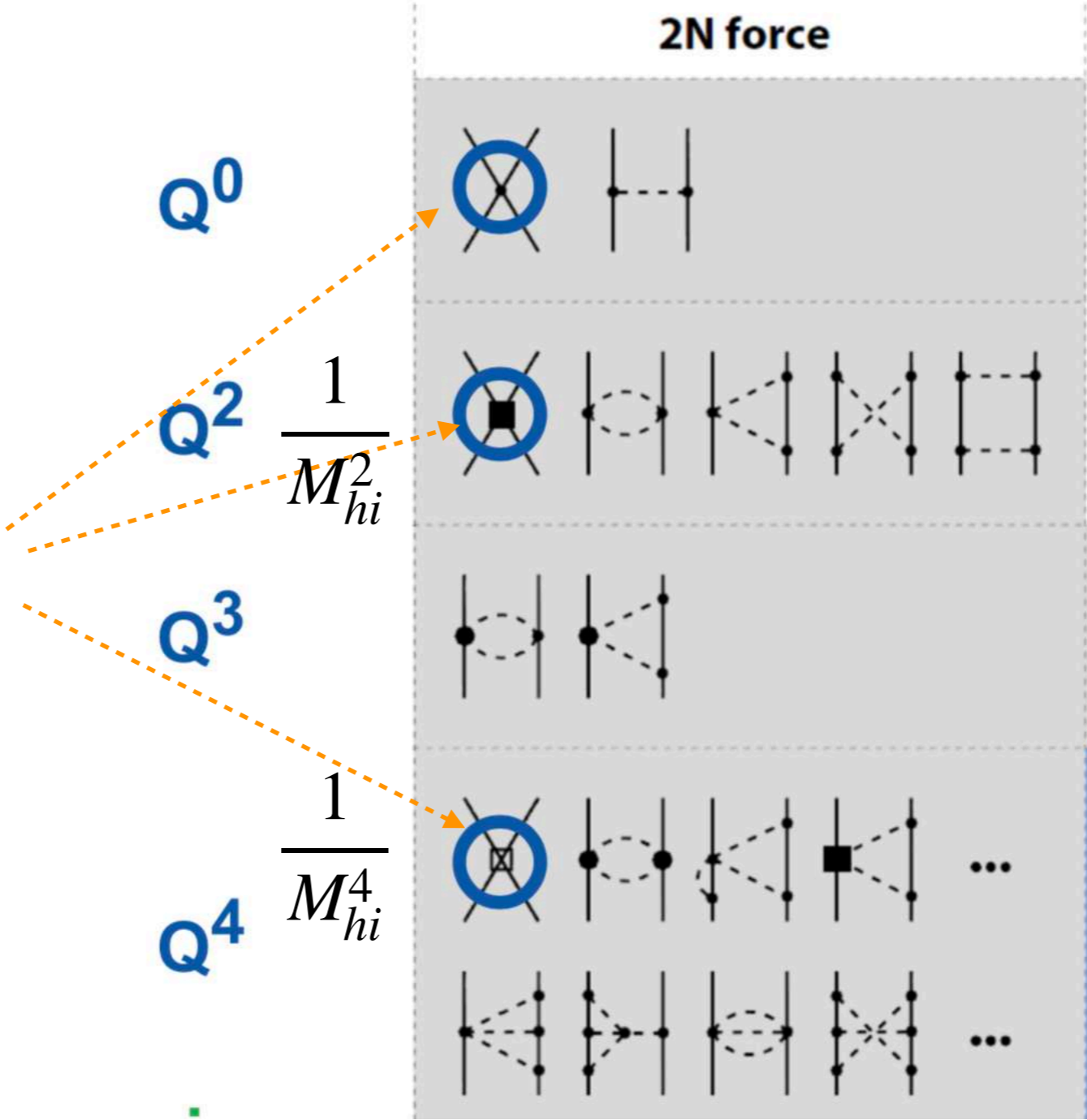
Power counting: short-range physics



- Strength of OPE $a_l f_\pi$ may have impact on contacts through renormalization
- Coexistence of $a_l f_\pi$ and M_{hi} makes NDA no longer reliable
- Operators gaining large anomalous dimension through nuclear dynamics \rightarrow “irrelevant” operators become relevant

Need to re-examine contact operators

24 contacts
in NDA up to Q^4

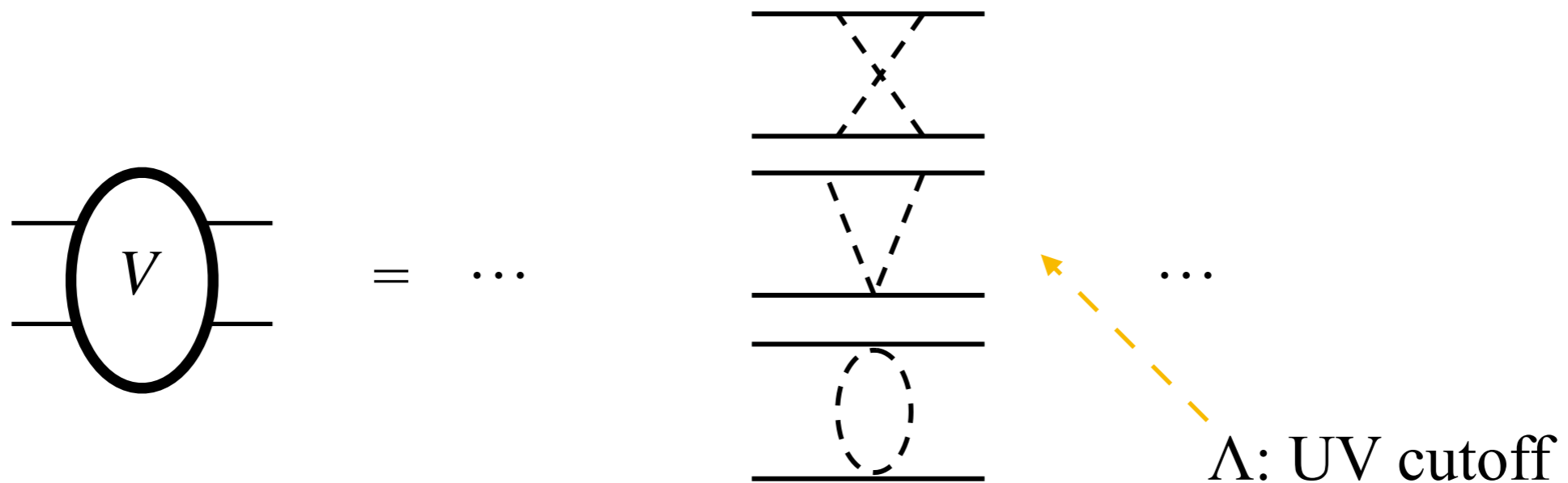


Counting short-range operators

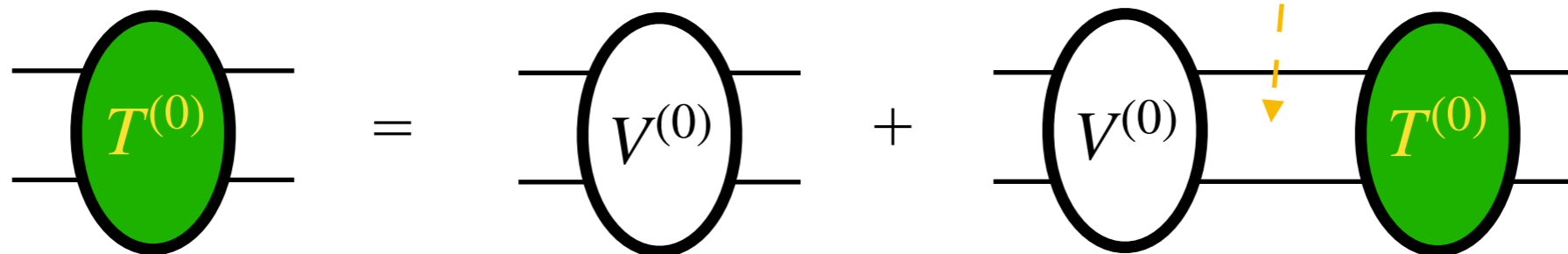
- At any given order in a power counting scheme, there must be enough operators to satisfy renormalization group invariance
 - ⇒ explicit checking UV cutoff independence
 - ⇒ model independence
- In terms of Wilson's RG
 1. Assume O be irrelevant (statement of PC)
 2. Run RGE
 3. Will O stay irrelevant in EFT?

What cutoff?

- Potentials: two-nucleon irreducible diagrams



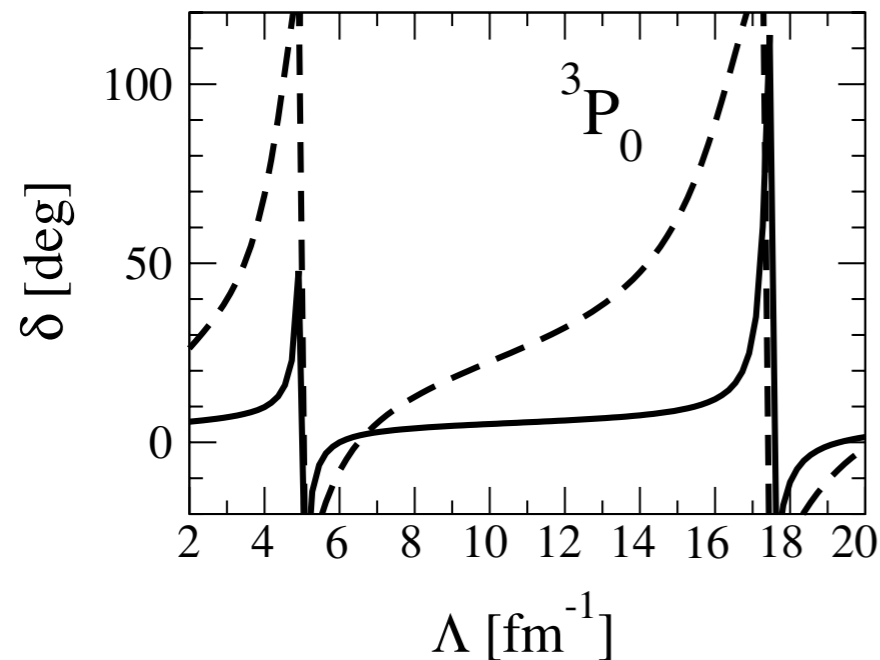
- Lippmann-Schwinger eqn (equivalent to Schrodinger eqn)



Renormalizing singular attraction

Nogga, Timmerman & van Kolck (2005)

Phase shifts vs. Λ



Solid: $T_{lab} = 10$ MeV, dashed: 50 MeV

$$C_{3P0} \vec{p} \cdot \vec{p}' \sim \frac{Q^2}{m_{hi}^2} \quad C_{3P0} \vec{p} \cdot \vec{p}' \sim \frac{Q^2}{m_{lo}^2}$$

$O(Q^2)$

$O(1)$

WPC

RG inv. counting

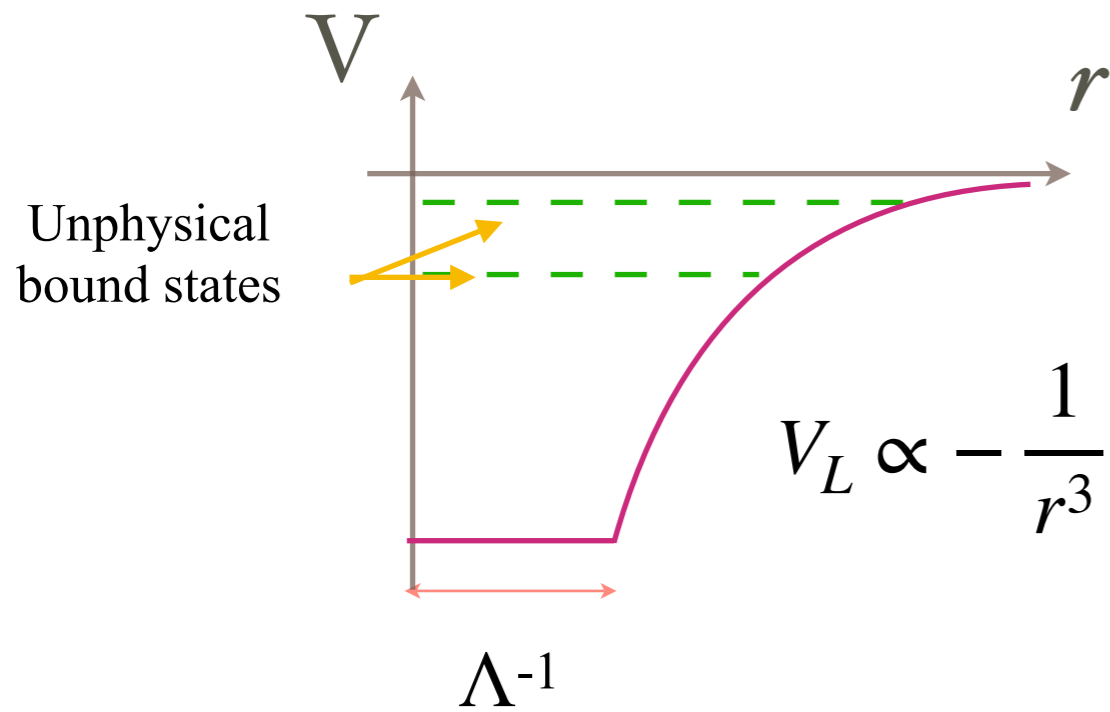
- Contacts needed at LO in attractive triplet channels: $3P2 - 3F2, 3D2, 3D3 \dots$

Renormalizing singular attraction

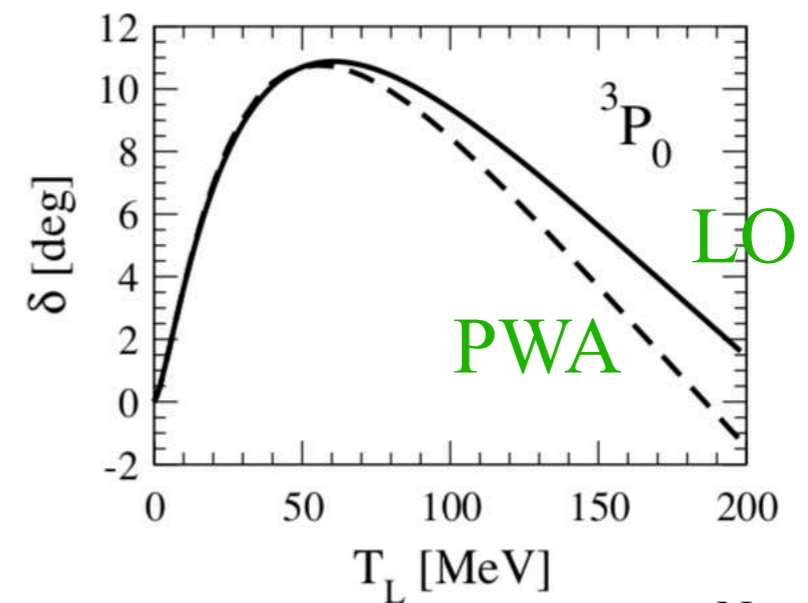
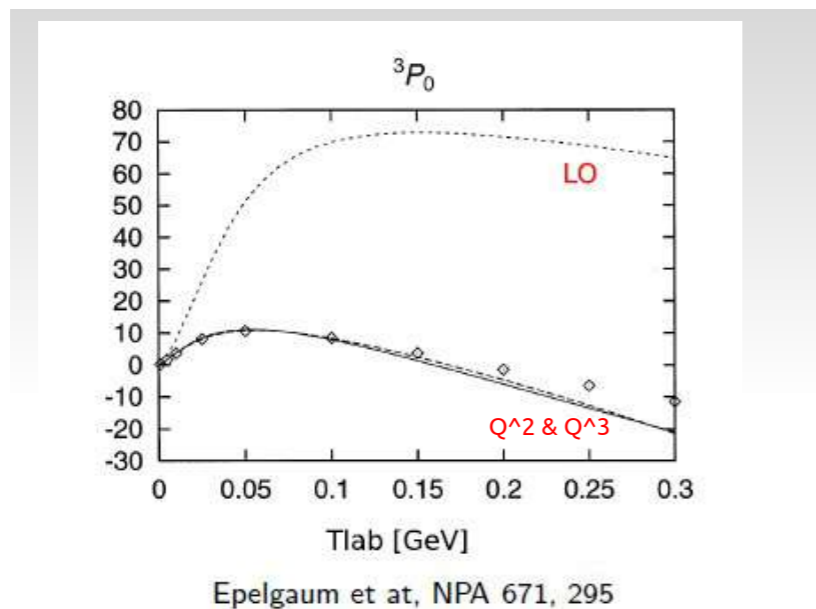
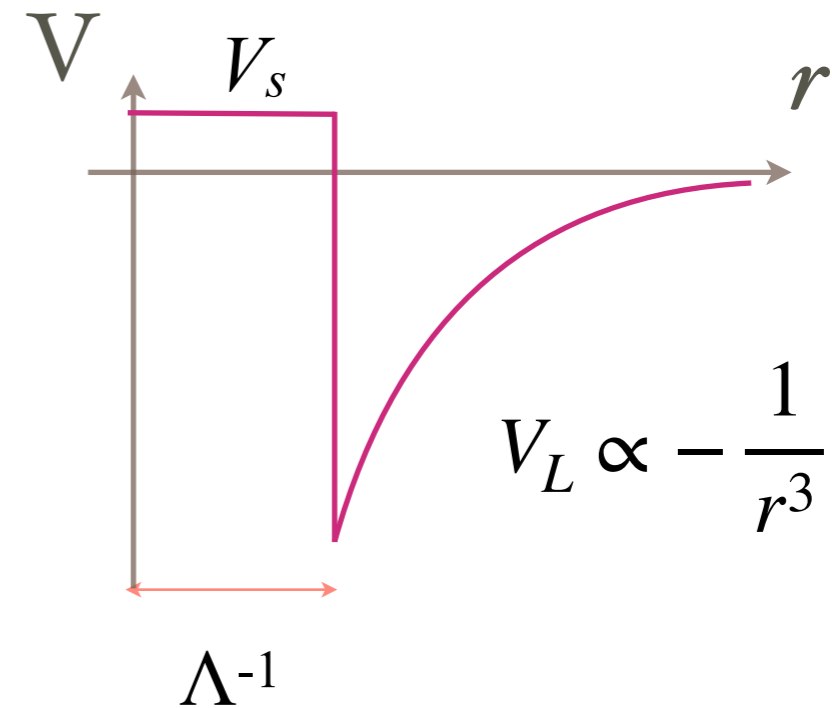
Beane et al ('01)

Pavon Valderrama & Ruiz Arriola ('05 ~ '07)

Nogga et al ('05)



Modify PC



Nogga et al ('05)

Modified power counting for chiral nuclear forces

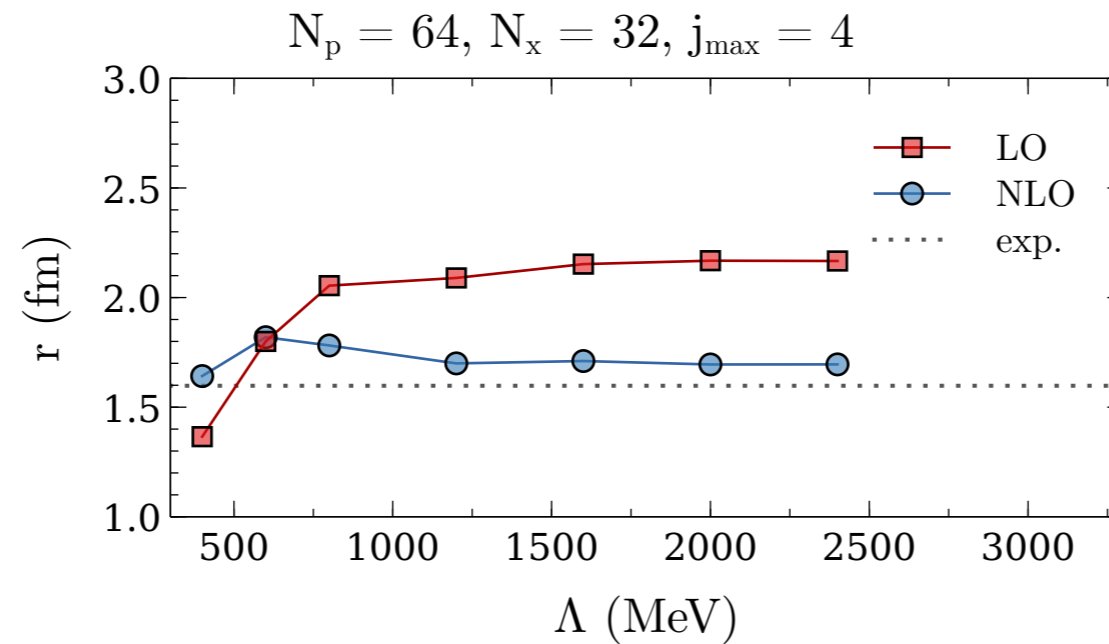
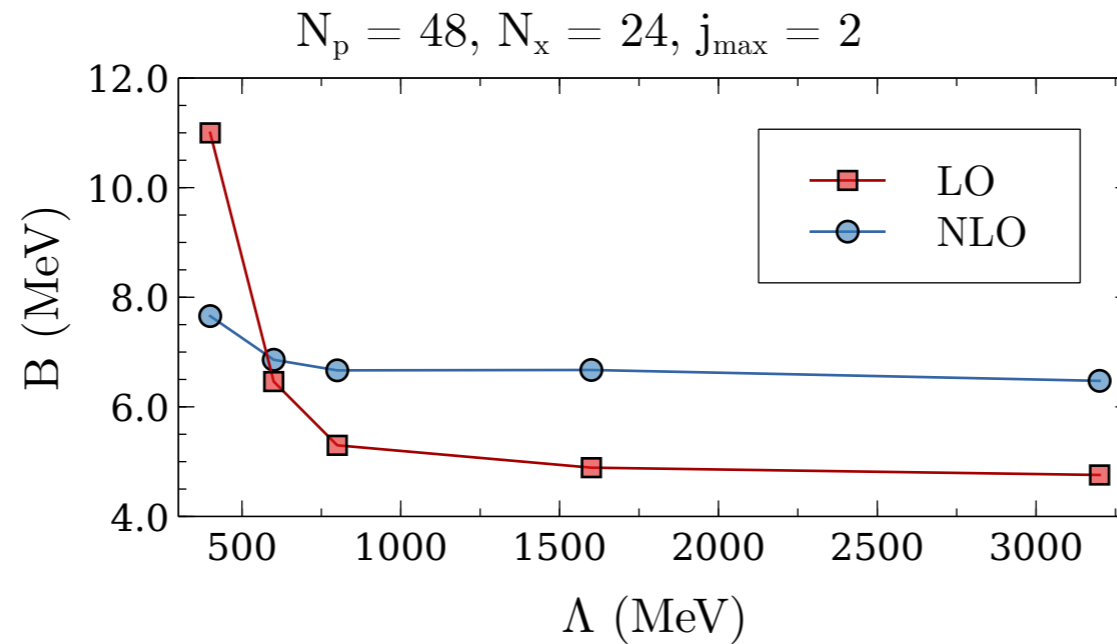
Nogga et al. '05

BwL & Yang '11, '12

Wu & BwL '19

- LO : (C + OPE) for 1S0, 3S1, 3P0 (perturbative OPE for most waves)
- NLO : Q^2 C.T. for 1S0; OPE for 1P1, 3P1, 3P2...
- N2LO: (Q^4 C.T. + TPE) for 1S0; (Q^2 C.T. + TPE) for 3S1-3D1 and 3P0
- N3LO:

Triton BE and charge radius Preliminary



nd elastic scattering

Preliminary

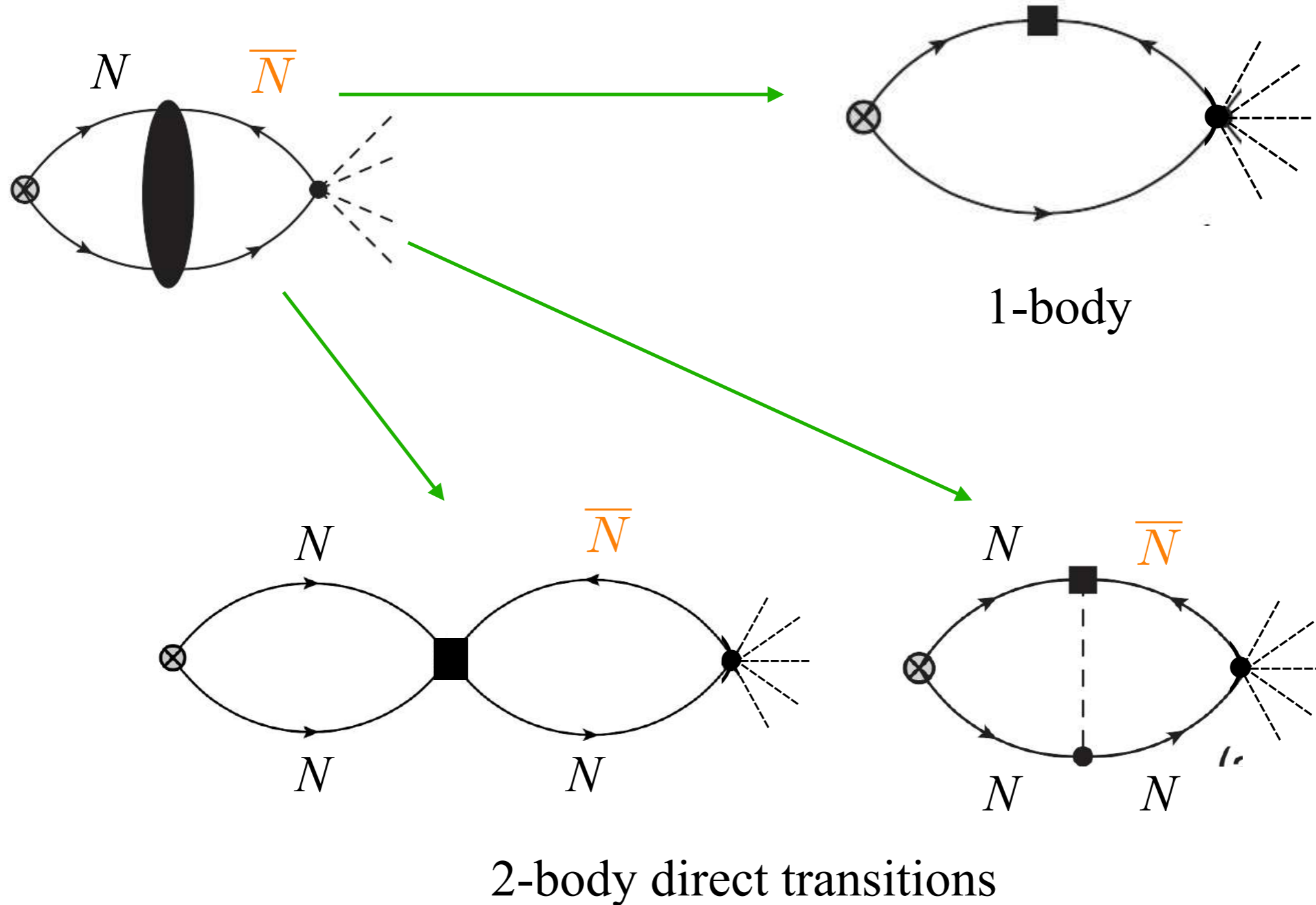
Phase shift in degrees ($j^\pi = 1/2^+$, S wave)

Tlab	1 MeV	2 MeV	3 MeV
LO	-20.2	-28.3	-37
NLO	-22.2	-33.1	-40.4
AV14	-17.8	-28	-34.9

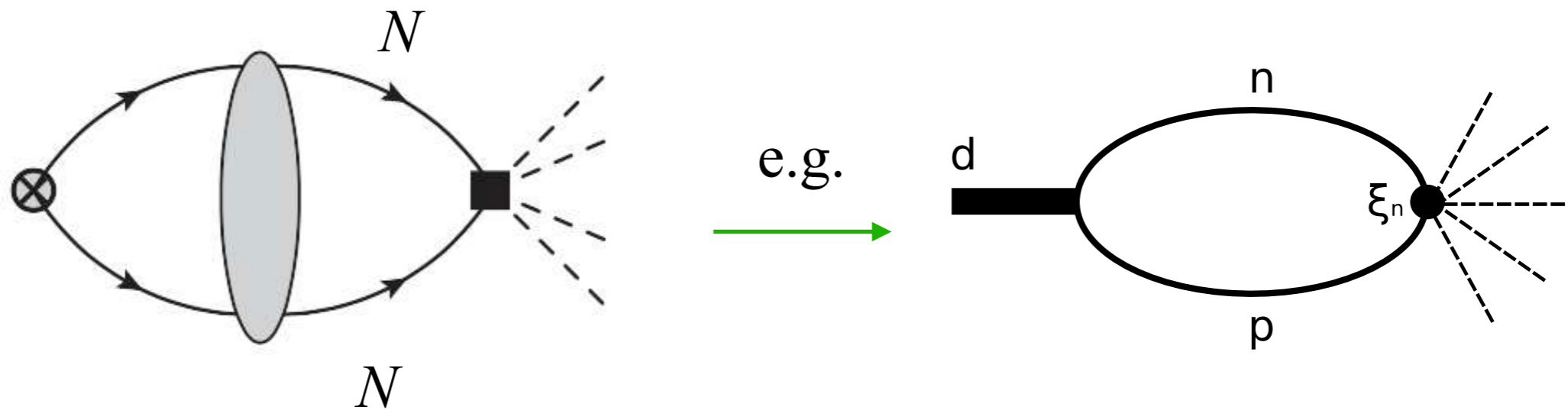
Deuteron decay by $NN \rightarrow NN\bar{b}$

Oosterhof, BWL, de Vries, Timmermans & van Kolck
PRL 122 (2019) 17, 172501

neutron-antineutron osc.



Direct NN annihilation



- To what extent can we disentangle these mechanisms?

Finally...

Oosterhof, BwL, de Vries, Timmermans & van Kolck
PRL 122 (2019) 17, 172501

$$R_d \equiv \Gamma_d^{-1} / \tau_{n\bar{n}}^2$$

$$R_d = - \left[\frac{m_N}{\kappa} \text{Im} a_{\bar{n}p} \left(1 + \overset{\text{NN range}}{0.40} + \overset{\text{Re}(a_{\bar{n}p})}{0.20} - \overset{\text{pion}}{0.13} \pm \overset{\text{NN} \leftrightarrow \text{N}\bar{\text{N}}}{\text{w/ unknown } B_0}{0.4} \right) \right]^{-1}$$
$$= (1.1 \pm 0.3) \times 10^{22} \text{ s}^{-1}.$$

- Perturbative pion allows for analytic expression
- Loosely bound neutron helps sensitivity (nuclei with neutron halo?)
- B_0 gives largest uncertainty
- W/ nonperturbative pion EFT, unknown LECs may have smaller impact

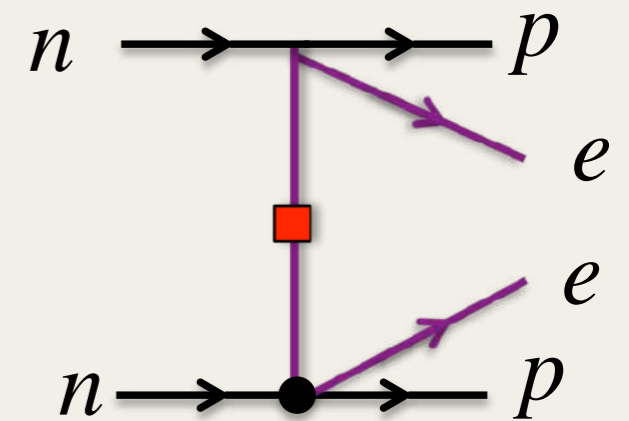
Chiral effective field theory

$\sim \text{GeV}$ $L = L_{QCD} + L_{Fermi} - m_{\beta\beta} \mathbf{v}_L^T C \mathbf{v}_L$ light quarks and gluons + electrons + neutrinos

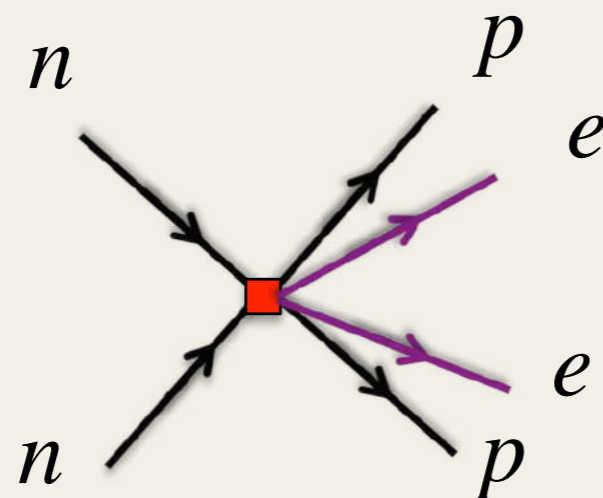
$\sim 100 \text{ MeV}$ Neutrinos are still degrees of freedom in the low-energy EFT

LO interaction : $\mathbf{v}_L \leftarrow \text{[red square]} \rightarrow \mathbf{v}_L \sim m_{\beta\beta}$

Leads to long-range $nn \rightarrow pp + ee \sim \frac{m_{\beta\beta}}{q^2}$
 $q \sim k_F \sim m_\pi$



'Hard' neutrino exchange $(E, |\vec{p}| > \Lambda_\chi) \rightarrow$ short-range operators

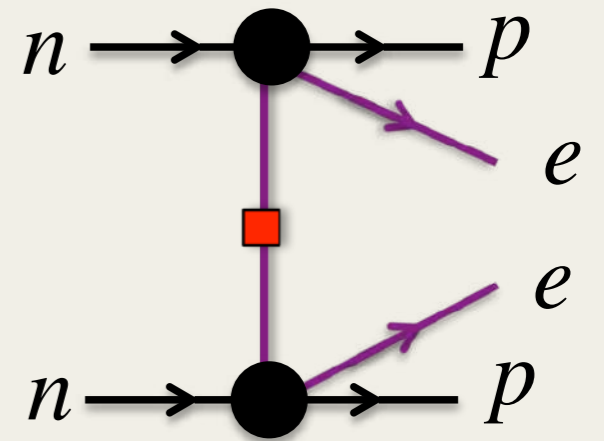


Expected at N^2LO

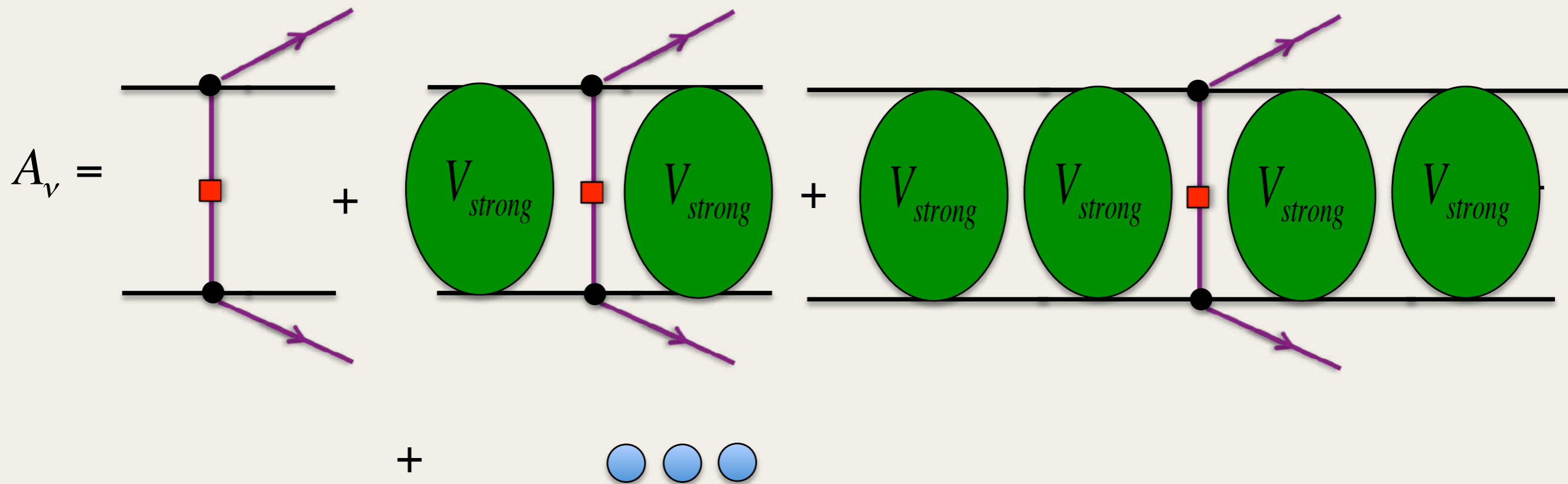
$$\sim \frac{m_{\beta\beta}}{\Lambda_\chi^2}$$

The neutrino amplitude

- At LO the 'standard' mechanism is long-range



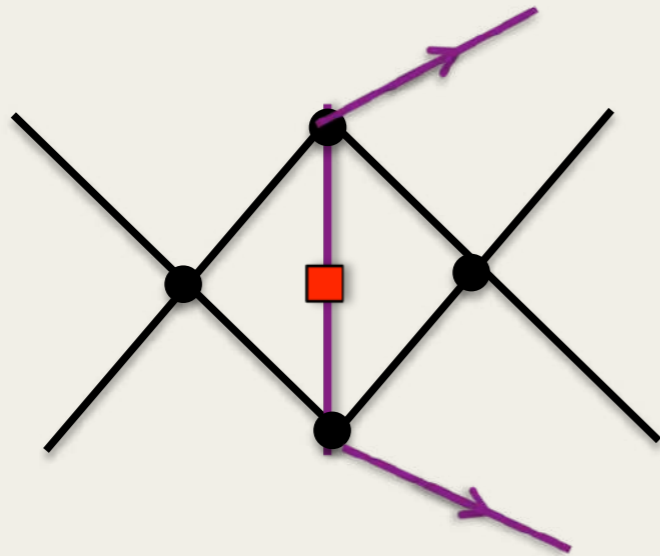
$$V_\nu = (2G_F^2 m_{\beta\beta}) \tau_1^+ \tau_2^+ \frac{1}{\vec{q}^2} \left[1 - g_A^2 \left(\vec{\sigma}_1 \cdot \vec{\sigma}_2 - \vec{\sigma}_1 \cdot \vec{q} \vec{\sigma}_2 \cdot \vec{q} \frac{2m_\pi^2 + \vec{q}^2}{(m_\pi^2 + \vec{q}^2)^2} \right) \right] \otimes \bar{e}_L e_L^c$$



Non-perturbative renormalization

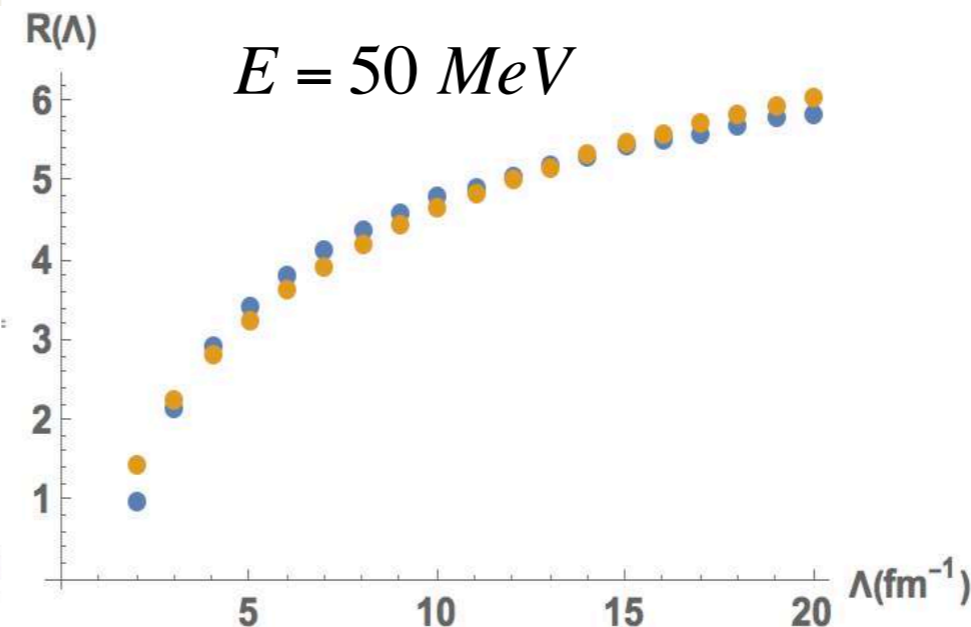
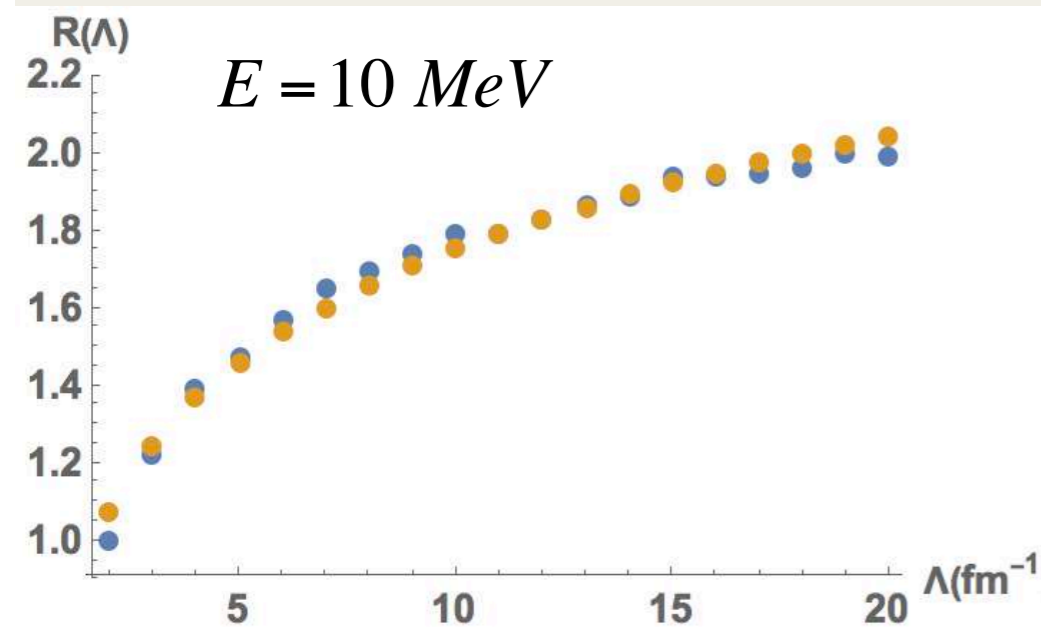
Kaplan et al '98

Can show analytically (dim-reg) two-loop diagram with two C_0 is UV divergent



$$\sim (1 + 2g_A^2) \left(\frac{m_N C_0}{4\pi} \right)^2 \left(\frac{1}{\varepsilon} + \log \frac{\mu^2}{p^2} \right)$$

Confirmed numerically for $nn \rightarrow pp + ee$ $R(\Lambda, E) = \frac{A_v(\Lambda, E)}{A_v(\Lambda = 2 \text{ fm}^{-1}, E)}$



● numerical result
 ● fit to:
 $R(\Lambda, E) = a + b \log(\Lambda \text{ fm})$

Summary

- Chiral EFT has infinite number of LECs
→ power counting is crucial
- NDA good for counting long-range physics, but unreliable for short-range interactions
- RG analysis (UV cutoff independence) can be used as guideline to test PC for short-range physics